

# Bandit Algorithm, Reinforcement Learning, and Horse Racing Result Prediction

**LYU2103**

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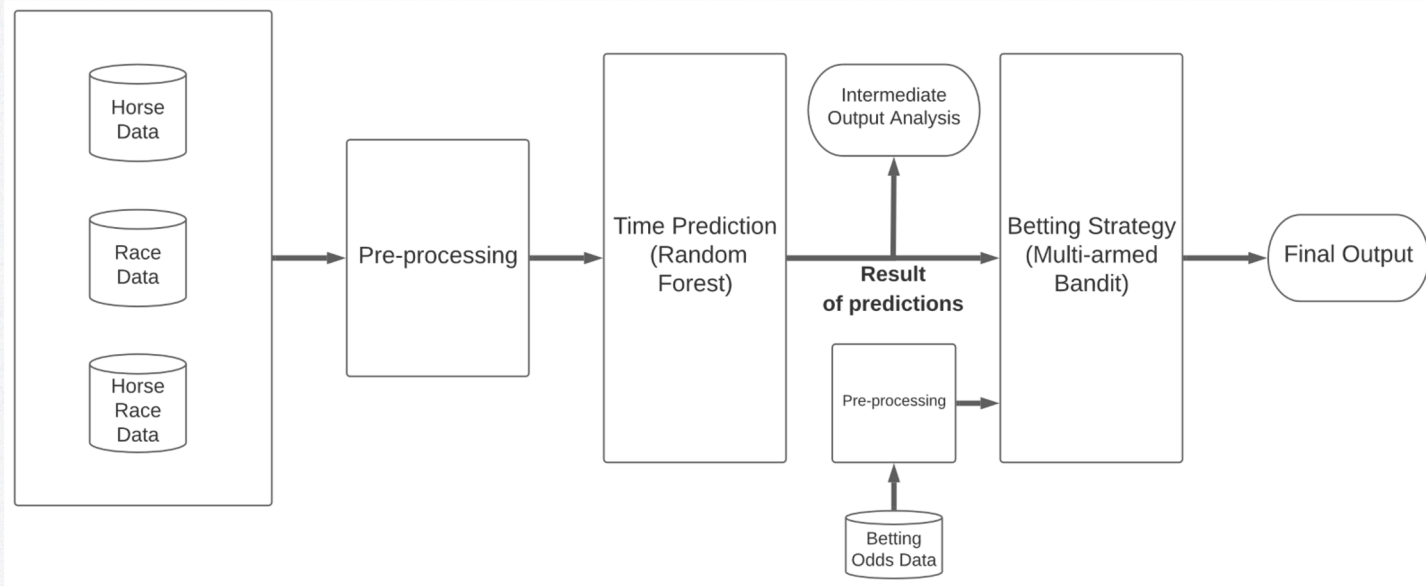


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# Review

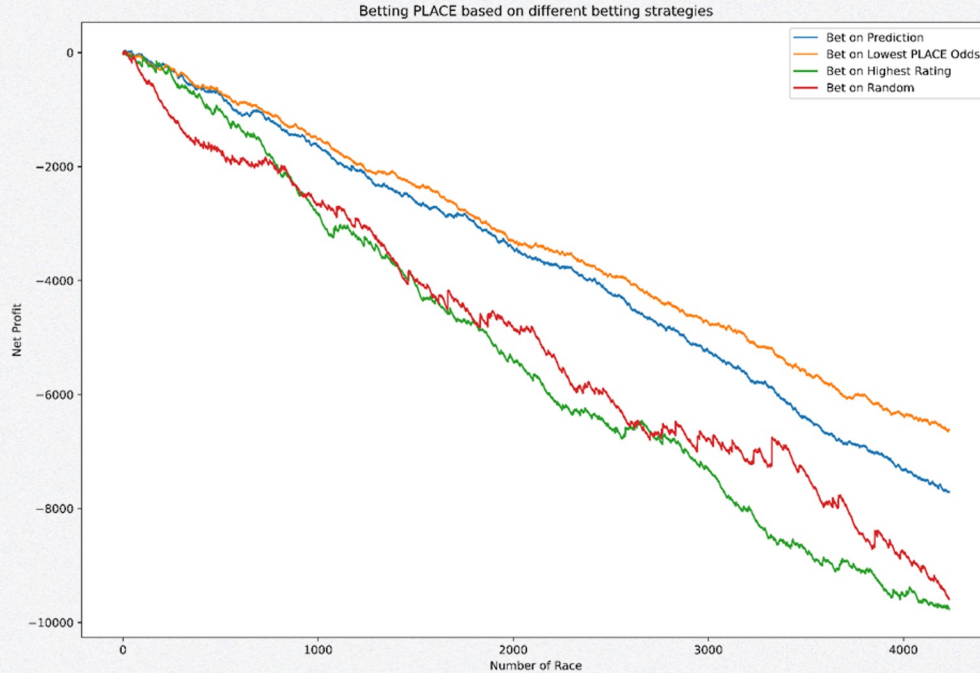
Achievements in Last Semester

# Recall that...





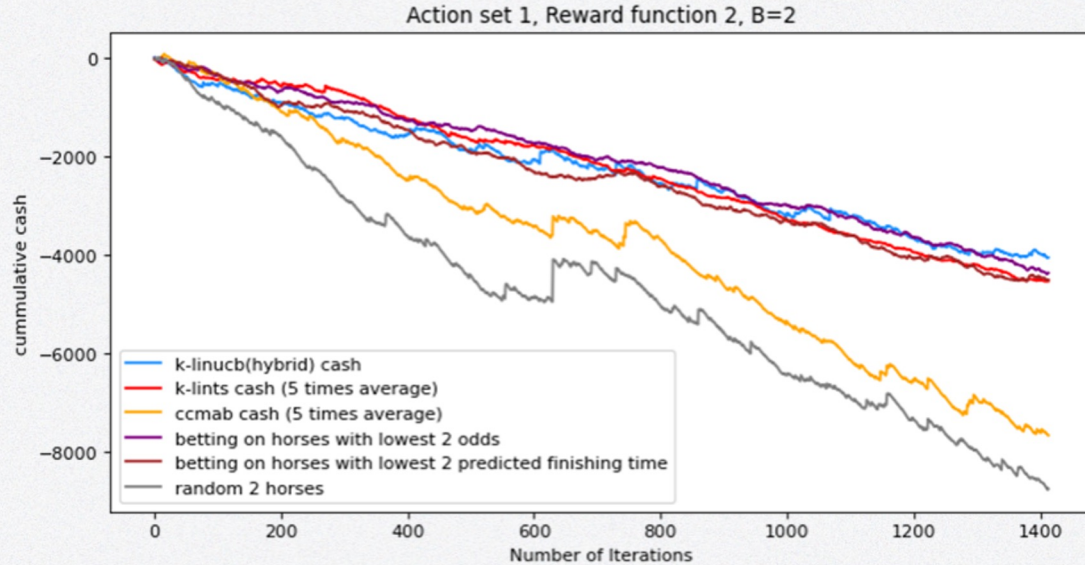
# Recall that...



Simulated horse betting on the time prediction result from the random forest model

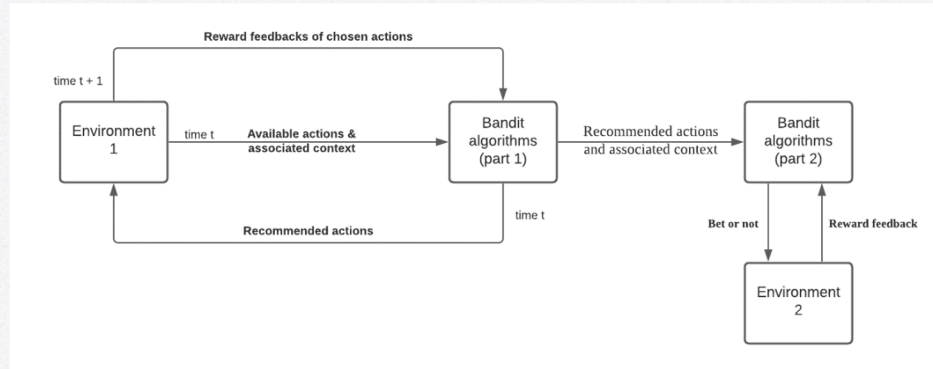


# Recall that...

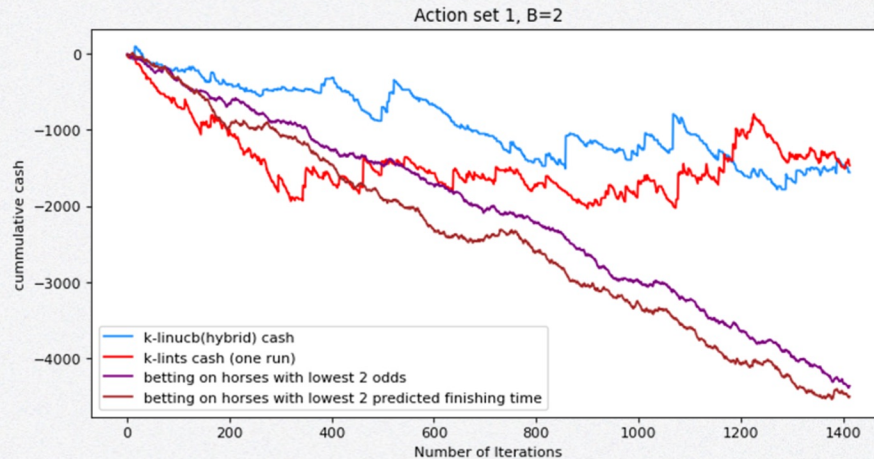


Explored different  
Bandit algorithms in  
many constructs (e.g.  
action sets, reward functions)  
On Horse betting

# Recall that...



Applied a tricky technique to attempt to let bandit algorithm decide how much to bet





# Agenda

**1**

**Introduction**

**2**

**Data**

**3**

**Horse Racing  
Prediction**

**4**

**Betting  
Strategies**

**5**

**Conclusion**

**6**

**Q&A**





**1**

# Introduction

Objectives, Contribution



# Objectives (2nd Semester)

- Improve **accuracy** and **interpretation** of time prediction model
- Explore new horse betting strategies using **new bandit algorithms** and **other** types of reinforcement learning algorithms
- Enable the agent **bet with different amount of money**
- Enhance the stability of horse betting strategies using **model selecting with EXP3**





# WHAT'S NEW?



# WHAT'S NEW?

1. Improved  
Random  
Forest Model
2. Explored  
New Bandit  
Algorithms
3. Applied More  
RL Algorithms  
on Horse Betting
4. Model  
Selection  
using Bandit  
Algorithm



# Contribution

1. Reduced loss of random forest betting
  - WIN bet
    - i. Reduced 87.162% loss**
  - PLACE bet
    - i. Reduced 46.008% loss**
2. Explored possible horse betting strategies generation (**PLACE**)
  - Neural Bandit / Neural UCB
  - Other reinforcement learning algorithms
3. **Enhanced stability** of horse betting strategies using model selection





# 2

# Data

Descriptions, Analysis & Pre-processing





# Sources & Descriptions

- **Data Sources**
  - a. The Hong Kong Jockey Club
  - b. Data Guru
  - c. hkHorse
- **Datasets**
  - Ranged from 1979 to 2021
  - Tables:
    - Races data
    - Horses data
    - Horse-race data
    - Betting odds data



# Input Data for Training

Features	Types	Encoding Methods
raceclass	Categorical	Ordinal
tracktype	Categorical	One-hot
racktrack	Categorical	One-hot
course	Categorical	One-hot
country	Categorical	One-hot
importtype	Categorical	One-hot
sex	Categorical	One-hot
colour	Categorical	One-hot
going	Categorical	One-hot
jockey	Categorical	Ordinal
trainer	Categorical	Ordinal
horseid	Categorical	Ordinal
dam	Categorical	Ordinal
sire	Categorical	Ordinal
damsire	Categorical	Ordinal
distance	Categorical	Ordinal
draw	Categorical	Ordinal
rating	Real Value	/
rating_rank	Real Value	/
last_rating	Real Value	/
avg_rating	Real Value	/
last_place	Real Value	/
winodds	Real Value	/
win_odds_rank	Real Value	/
actualweight	Real Value	/
declaredweight	Real Value	/
gear	Categorical	Customized Encoding
raceidseason	Real Value	/
count_{1 - 3}	Real Value	/
weight_diff	Real Value	/
avg_finishtime	Real Value	/
avg_pos{1 - 6}_pos	Real Value	/
avg_pos{1 - 6}_time	Real Value	/
last_pos{1 - 6}_pos	Real Value	/
last_pos{1 - 6}_time	Real Value	/

- Features included
  - Races data
  - Horses data
  - Horse-race data
  - Additional features
- Drop unnecessary , irrelevant features
- Split train and test data according to race season
  - **Training** data: **2008 - 2019**
  - **Testing** data: **2019 - 2021**





**3**

# Horse Racing Prediction

Procedure, Evaluation & Performance

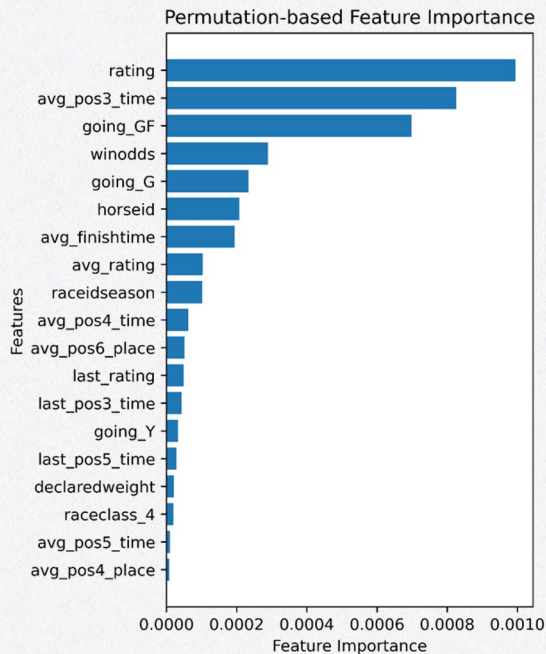
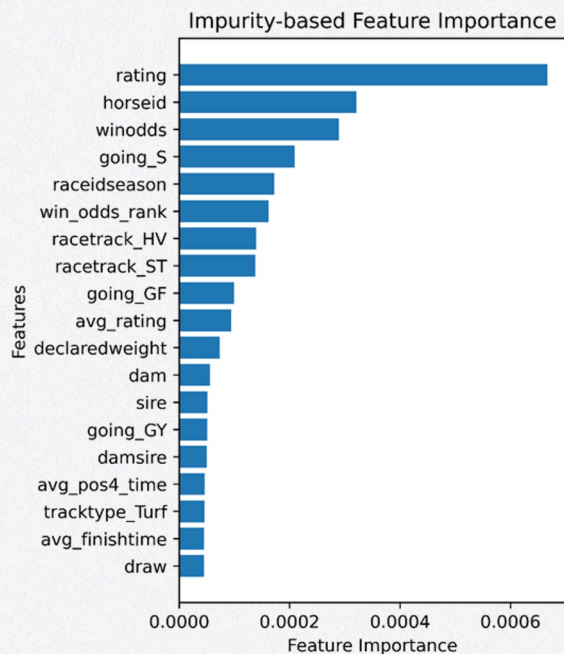




# A New Random Forest



# Why Need This?



- Some features are **not influential**
- Some features are **correlated**
- **Improve accuracy** of the model
- Investigate the importance of features **among the selected features**

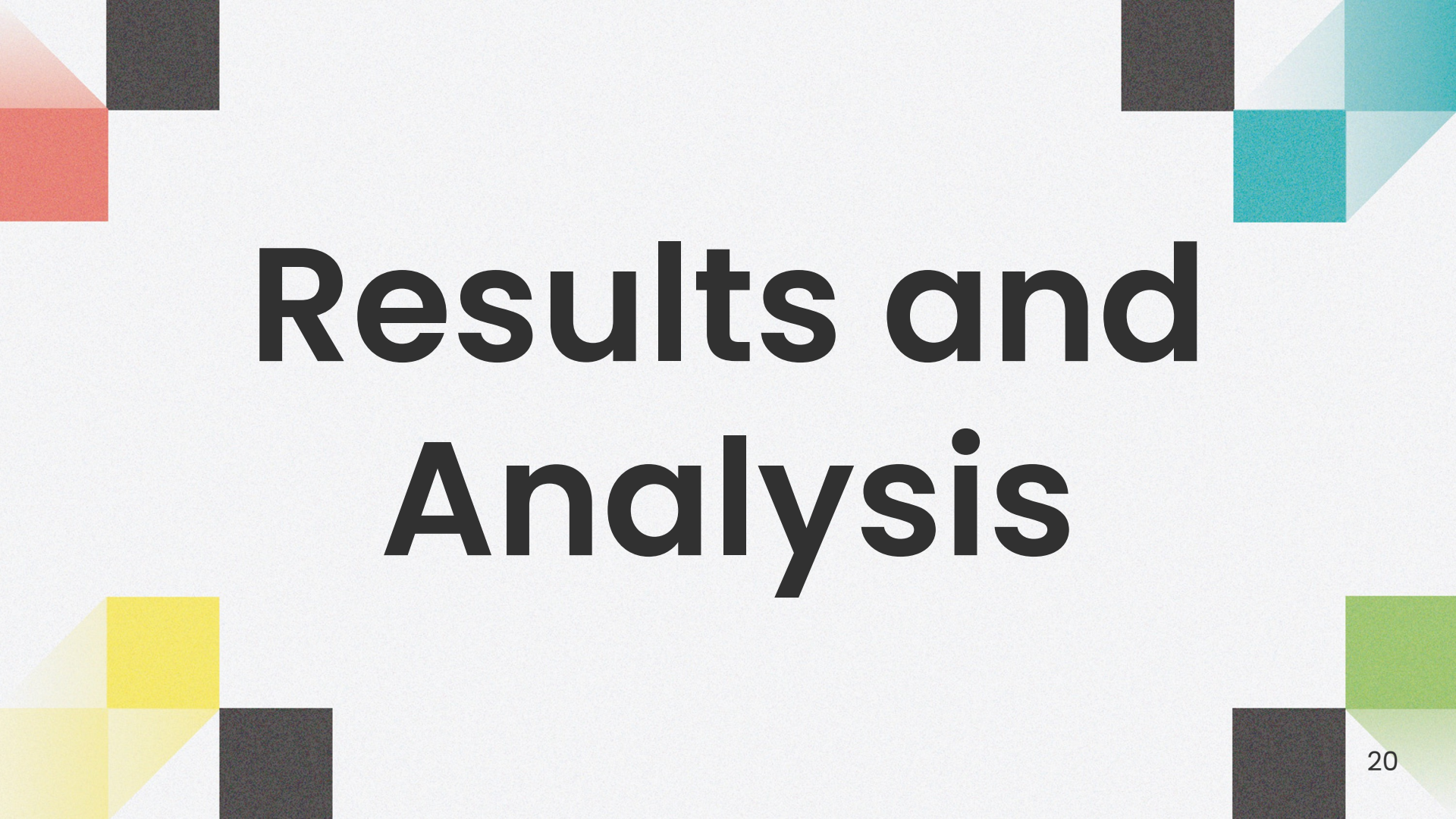


# Features of New Model

Features	Types	Encoding Methods
raceclass	Categorical	Ordinal
horseid	Categorical	Ordinal
distance	Categorical	Ordinal
rating	Real Value	/
winodds	Real Value	/
win_odds_rank	Real Value	/
raceidseason	Real Value	/

- Features included
  - Horses data
  - Horse-race data
- Extract features with **7 highest importance**
- Split train and test data according to race season
  - **Training** data: **2008 – 2019**
  - **Testing** data: **2019 – 2021**





# Results and Analysis



# Evaluation Metrics

- **Mean Squared Error (MSE)**
  - Accuracy of the prediction
  - Closer to 0, the better performance
  - **MSE of model: 1.7177 seconds**
    - **reduced by 24%** with value of **0.5472**
- **Explained Variance Score**
  - Discrepancy between the model and data
  - The closer to 1, the stronger association
  - **Explained Variance Score of model: 0.99547**
    - **increased by 0.00159**



# Betting Accuracy

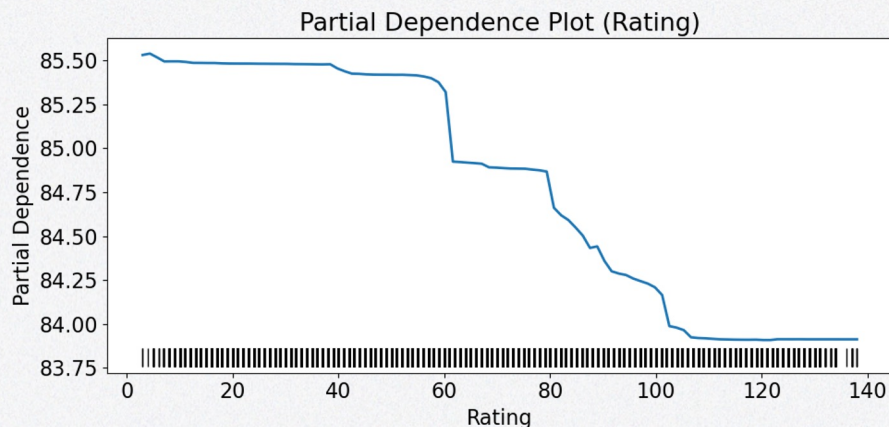
- **WIN Betting**
  - Correctly predicted 24.331% of races
    - **Decreased by 0.206% from old model**
- **PLACE Betting**
  - Correctly predicted 47.108% of races
    - **Decreased by 0.499% from old model**



# Partial Dependence Plot (Rating)

Table 1.1 Rating for Race classes [57]

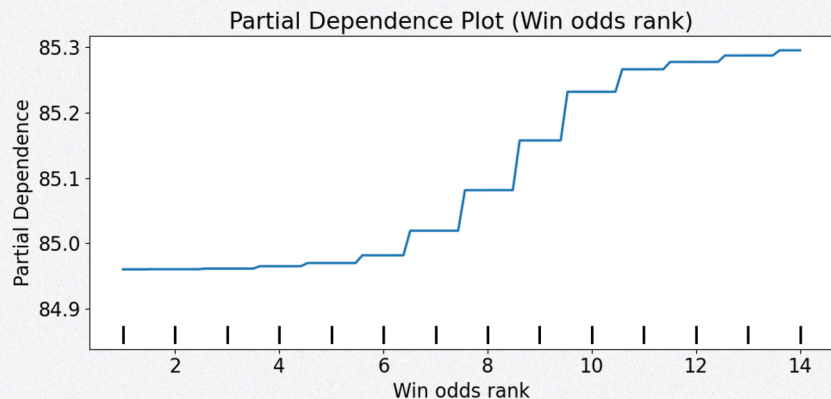
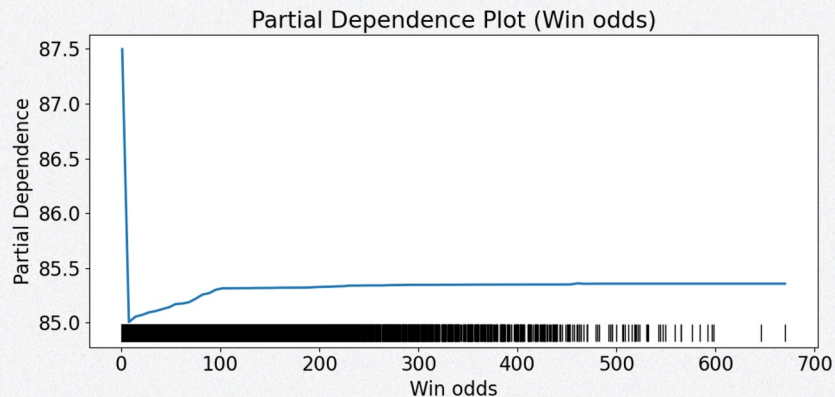
Rating upper bound	Race classes
120	1
100	2
80	3
60	4
40	5



- Rating has **highest feature importance**
- Race classes determined by rating
- **Inversely proportional** to finishing time
- Clear intervals in PDP
  - Matches race classes
- **Race class 2** has the most varied results



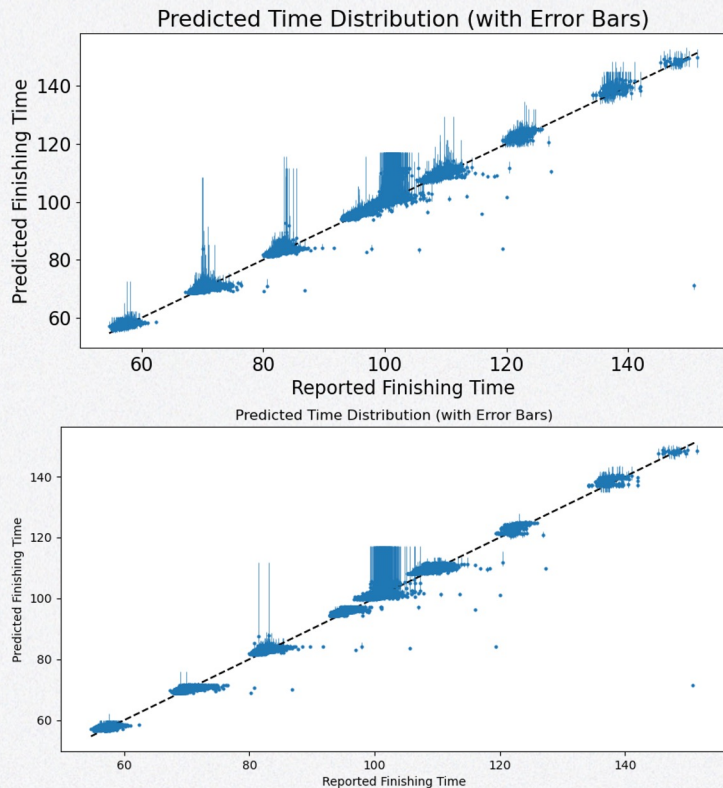
# Partial Dependence Plot (Odds)



- Win odd regards as public intelligence
- **Greatly dropped at low win odds**
  - Horses with low odd may not always win
- Win odd rank shows clear intervals
  - Rank 5 – 11 has a large step up



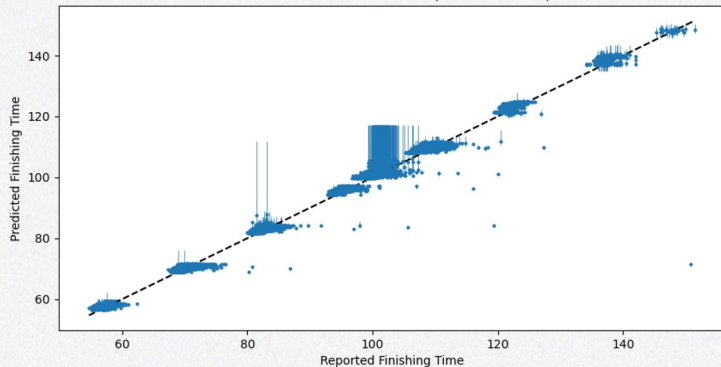
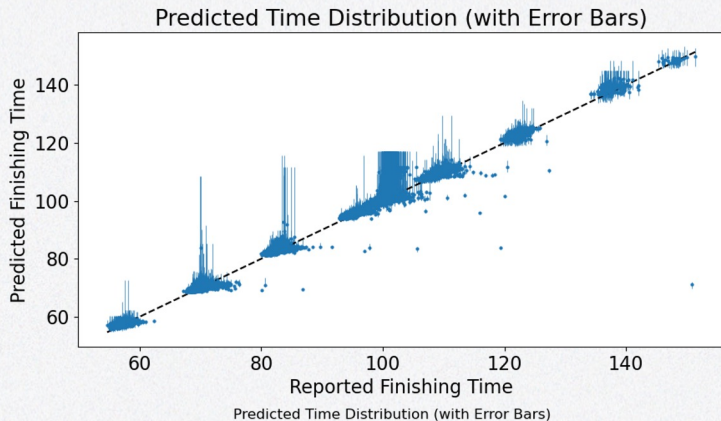
# Error Range of Predictions



- **Variance of predictions better than old model**
- Average range of predictions: **0.851s**
  - Reduced by **48.188%** from old model
- 22.397% of predictions **range > mean**
  - Reduced by **4.08%** from old model



# Error Range of Predictions



- Bet only predictions with small variance
  - **Range < mean**
  - Reduce loss
- **Change of number of correct predictions**
  - **WIN: Unchanged**
  - **PLACE: -5.2%**



# Betting Simulation

1. Group all the horses by the race
2. Order the horses by the predicted finishing time in ascending order
3. Assign a **predicted place** to each horse according to the ranking
4. Start Betting!

horseid			raceid	place	winodds	pred	pred_place	place_difference
17995	5265.0	2019-09-01-001-1600-Turf		1	2.2	95.84	1	0
17996	5186.0	2019-09-01-001-1600-Turf		2	4.9	95.89	4	2
17999	4302.0	2019-09-01-001-1600-Turf		3	18.0	96.16	5	2
17994	4268.0	2019-09-01-001-1600-Turf		4	5.7	95.86	3	-1
17993	4296.0	2019-09-01-001-1600-Turf		5	7.0	95.85	2	-3
18001	4809.0	2019-09-01-001-1600-Turf		6	19.0	96.21	7	1
17997	5103.0	2019-09-01-001-1600-Turf		7	50.0	96.35	9	2
17998	4845.0	2019-09-01-001-1600-Turf		8	14.0	96.33	8	0
18000	4982.0	2019-09-01-001-1600-Turf		9	21.0	96.17	6	-3



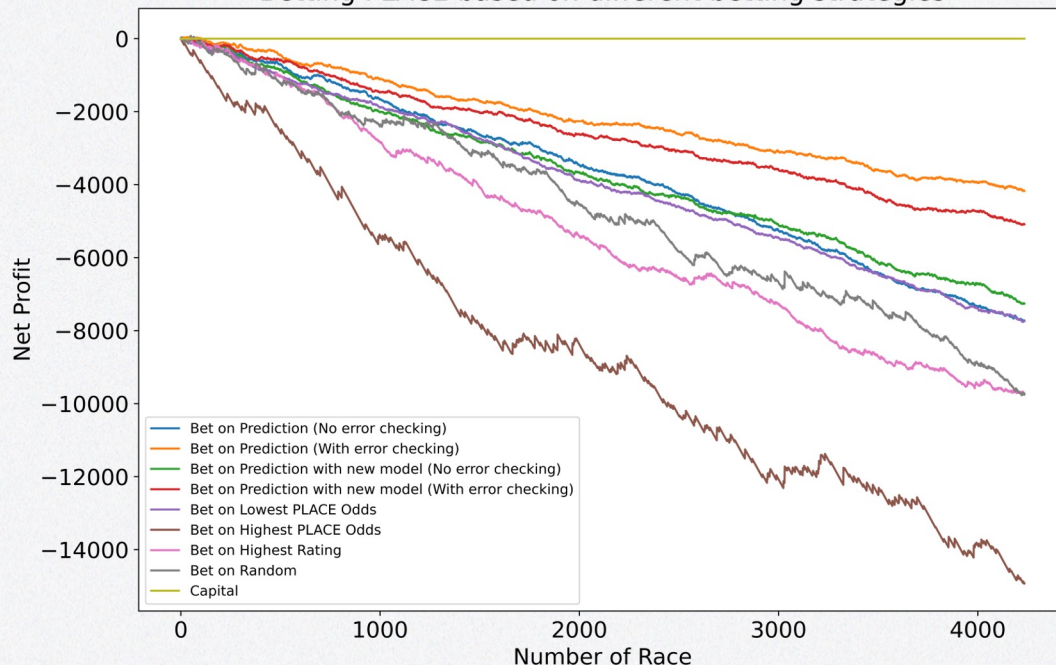
# Betting Simulation

1. Assume \$10 would be used for each bet
2. Gain **\$10 \* odds - 10** if correctly picked the horses
3. Lose \$10 otherwise
- 4. PLACE** betting would be simulated
5. Compare with different strategies
  - Based on lowest odds
  - **Based on highest odds**
  - **Based on error range**
  - Based on highest rating
  - Random



# Betting Simulation

Betting PLACE based on different betting strategies



- Betting **PLACE**
- Based on **Highest odds** is the worst
- **New model performs better (No error checking)**
- Based on **Error range** is the best
  - **Old Model** has **39.873%** accuracy
  - **New Model** has **41.914%** accuracy





**4**

# Horse Betting Strategies





# Bandit part Improvements



# Use better models

**Last Sem:** Linear models

Possible Problem: lower accuracy

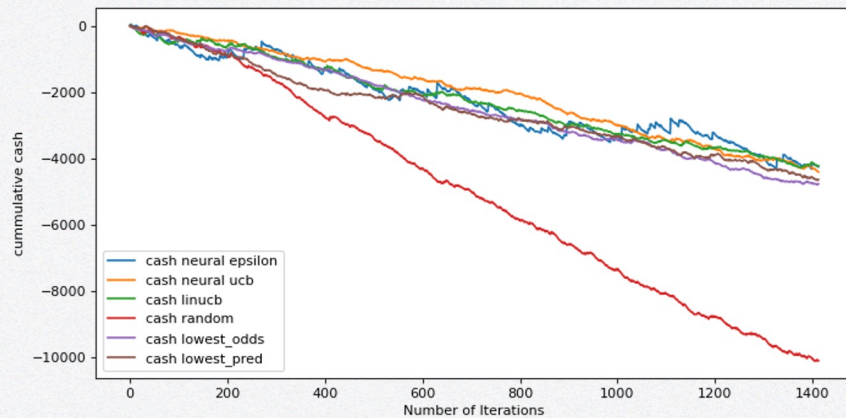
## **Attempt:**

Use more complex models: **neural networks**

- **Neural UCB** (Single neural network & UCB exploration)
- **Neural Bandit** (neural network committee & epsilon greedy exploration)



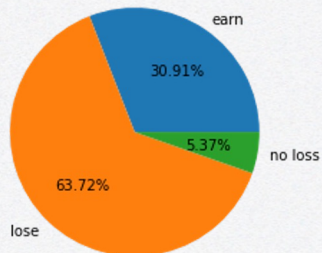
# Use better models



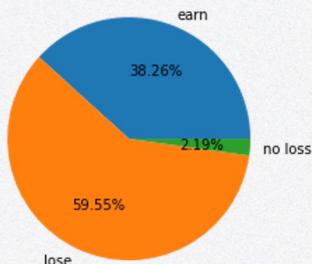
**Doesn't** show significant Improvement in terms of Cash balance

However, the earn rate is **8%** higher than that of linUCB

Percentage of games that earn by linUCB

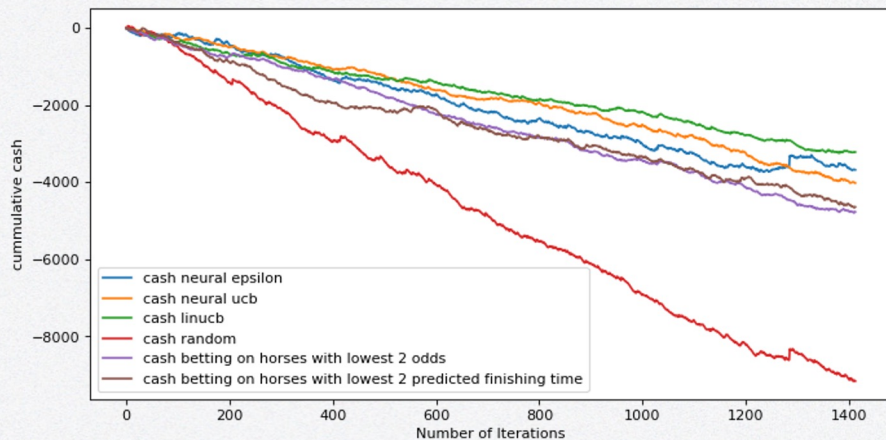


Percentage of games that earn by neural ucb





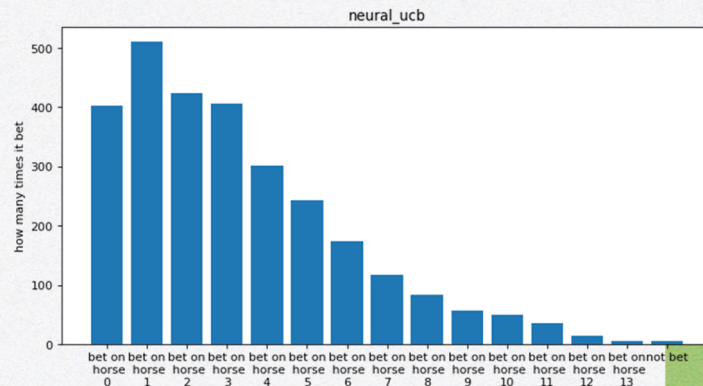
# Bets on fewer options



As top 5 horses occupy most out of all horses bet

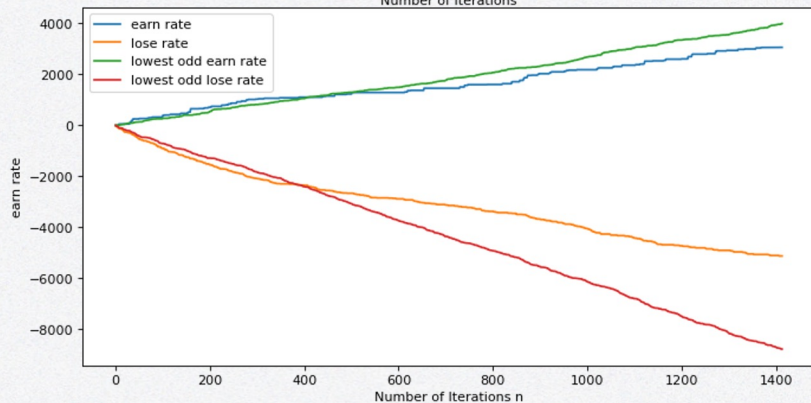
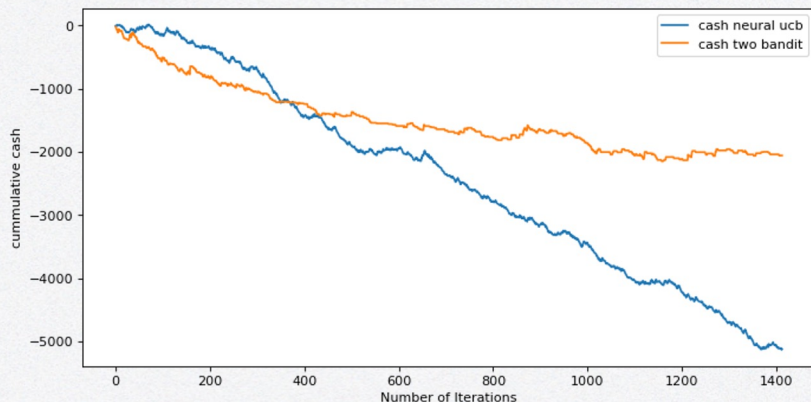
Bet on **only top 5**

- Slight improvements but still losing





# Redoing previous approach with these improvement



- Maintain its balance  
But doesn't earn
- Earn rate still grow  
overtime
- Lose rate reduces over time



# Concluding bandit parts

Problems of directly using bandit algorithms on horse betting:

- **Not flexible**
  - unable to consider state information like remaining balance
  - Not easy to make variable amount of bet  
(Directly set as actions: **Failed**, always fall to **safest** option which is \$10 bet)
- **Not work for very low odds and insufficient accuracy**
  - Low expected return

Might be better to use more common RL algorithms





# Other Algorithms



# Why using other algorithms?

- Explore the possibility of finding horse betting strategies using different algorithms
  - Enhance the profitability
  - Able to bet with different amounts of money
- Evaluate the performance of multi-armed bandit by comparing all results



# Algorithms used

- Selected from previous projects
  - Deep Q Network
  - Proximal Policy Optimization
- Other model-free, policy-based algorithms
  - Augmented Random Search
  - Cross Entropy Method



# Environments

**Type 1: only bet with \$10**

**Type 2: bet with different amount of money (\$10 – \$50)**

**Data to Use**

- Split into train and test set with 707 records each

**Features (for each horse):**

- Last moment place odds
- Last 10 minutes EMA of odds
- Rankings (odds, predicted finishing time)
- Ratio of finishing time between each horse with the horse ranked 1 place ahead (finishing time)
- Confidence level related (error range, upper and lower bound)



# Environments (Type 1)

## Action Set

- 14 horses (at most) ordered by predicted finishing time  
+ not to bet

## Terminating State

- No more races
- **Cash balance  $< 9000$**

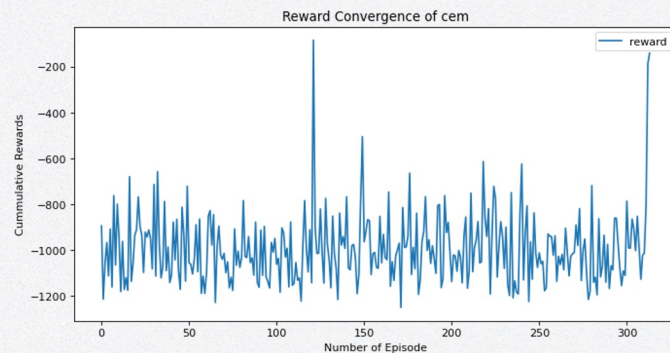
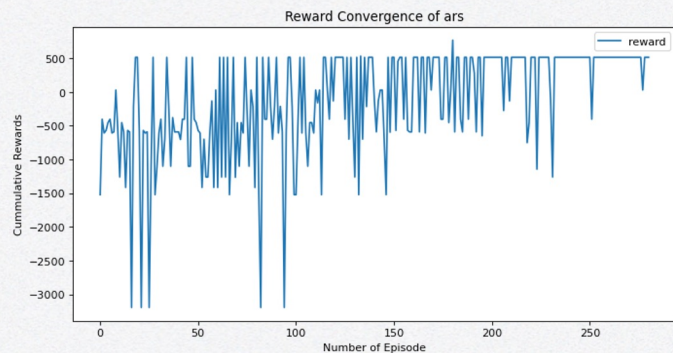
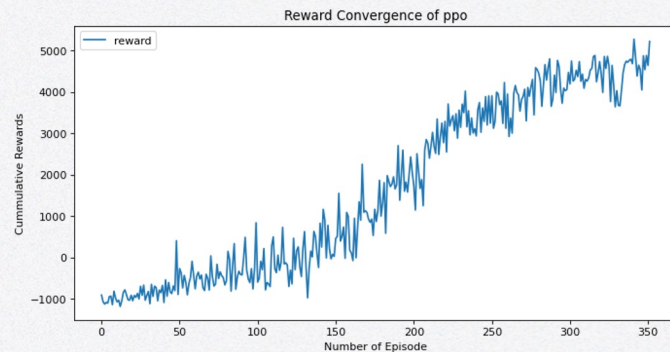
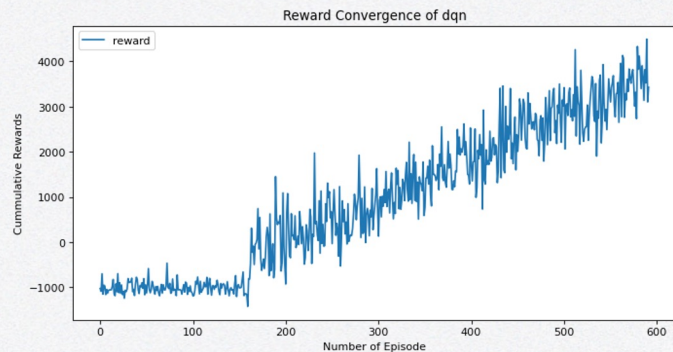


# Reward Functions (Type 1 & 2)

- $R(\text{Bet } \mathbf{\text{any of top 3}} \text{ horses correctly and } \mathbf{\text{error range}} < \mathbf{\text{mean}}) = (\text{dollar bet} * \text{betting odd}) * ((\text{dollar bet} / 10) + 0.5)$
- $R(\text{Bet } \mathbf{\text{any of top 3}} \text{ horses correctly}) = \text{dollar bet} * \text{betting odd of betted horse}$
- $R(\text{Bet wrong and } \mathbf{\text{error range}} > \mathbf{\text{mean}}) = -\text{dollar bet} * ((\text{dollar bet} / 10) + 0.5)$
- $R(\text{Bet wrong}) = -\text{dollar bet}$
- $R(\text{Not bet}) = -3$

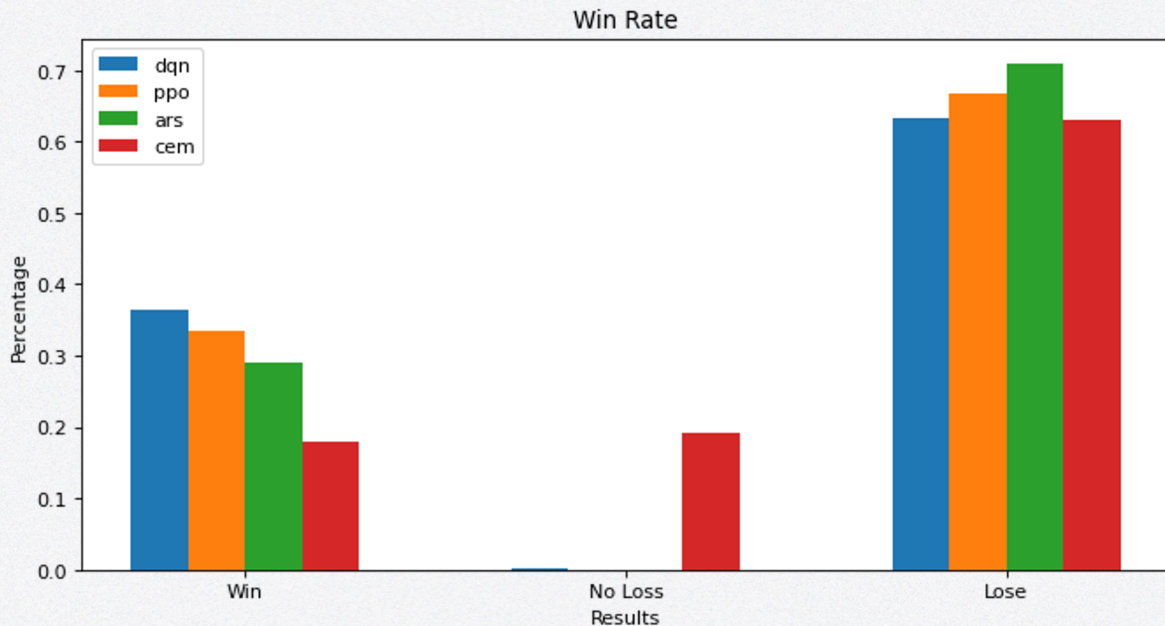


# Reward Convergence (Type 1)





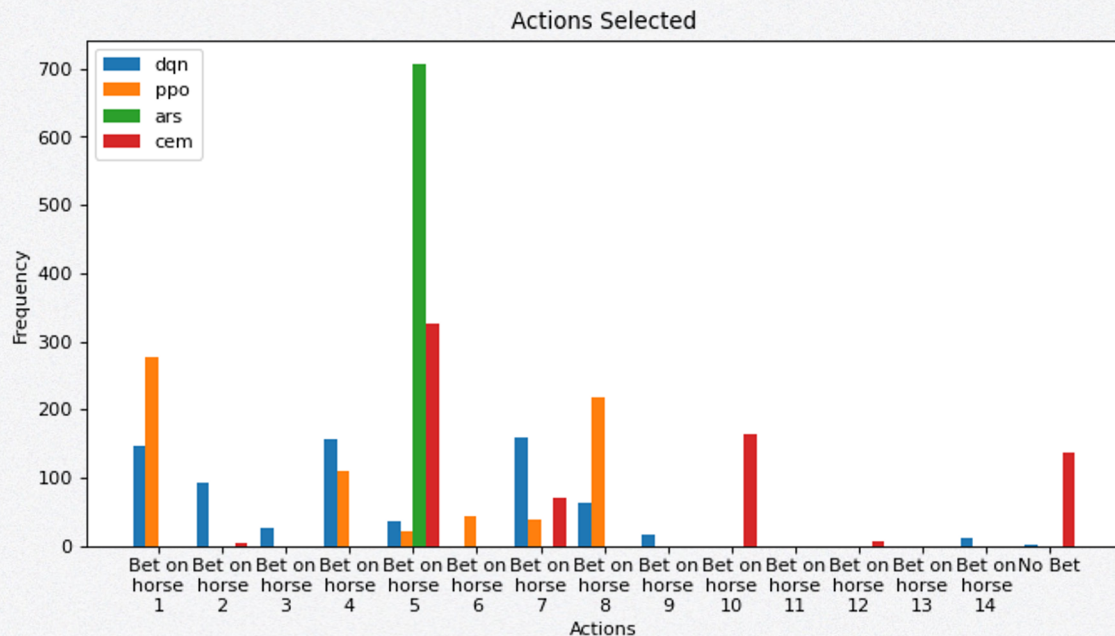
# Win Rate (Type 1)



- **DQN** has **highest** win rate
- **ARS** has **highest** loss rate
- **Majority** of selection are **betting**



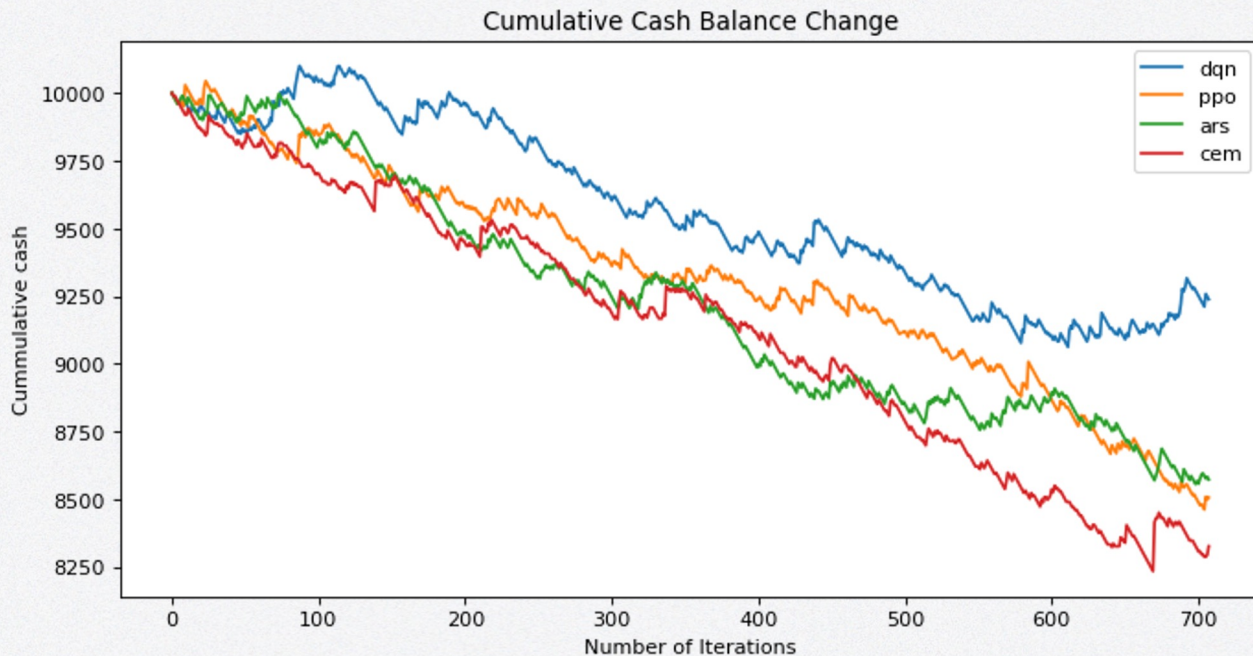
# Actions Selected (Type 1)



- Only **ARS** bet on **single option**
- **DQN & PPO** has a **safer** strategy
- **CEM**'s strategy involves **different risks**



# Profitability (Type 1)



- **All losing money**
- **DQN** perform **significantly better** than others



# Environments (Type 2)

## Action Set

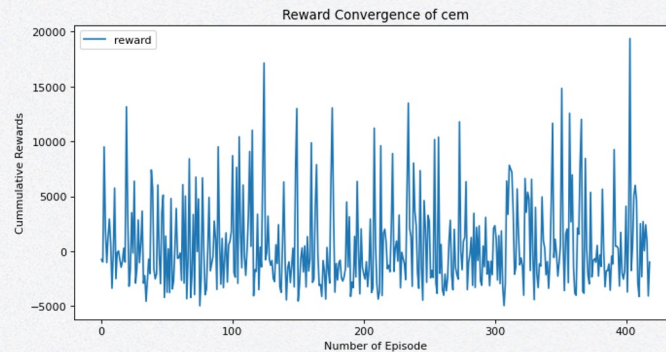
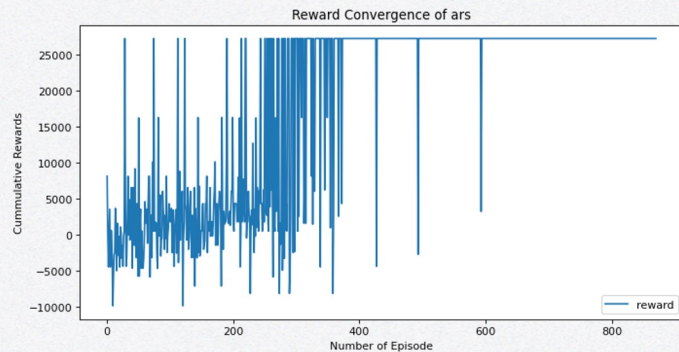
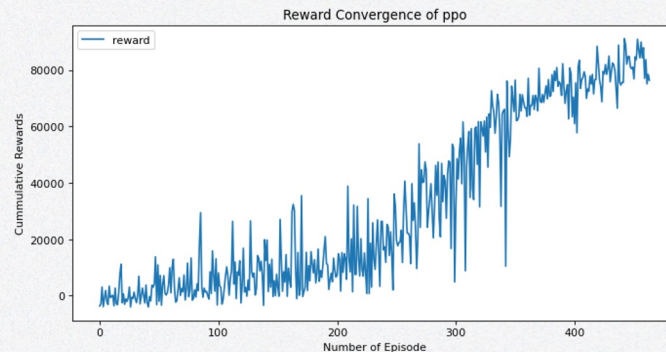
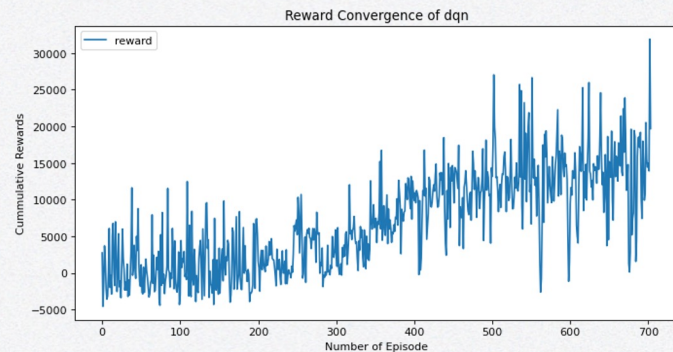
- 14 horses (at most) ordered by predicted finishing time + not bet
- 5 different amount of dollar bets (\$10, \$20, \$30, \$40, \$50)
- Total actions:  $15 * 5 = 75$

## Terminating State

- No more races
- **Cash balance  $< 8000$**

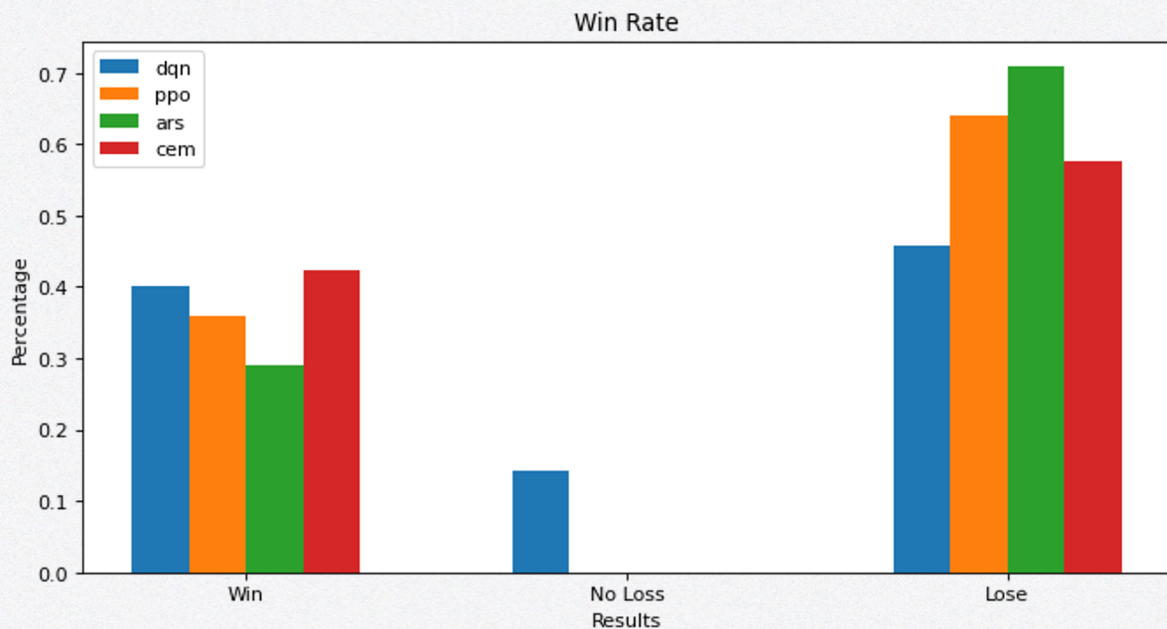


# Reward Convergence (Type 2)





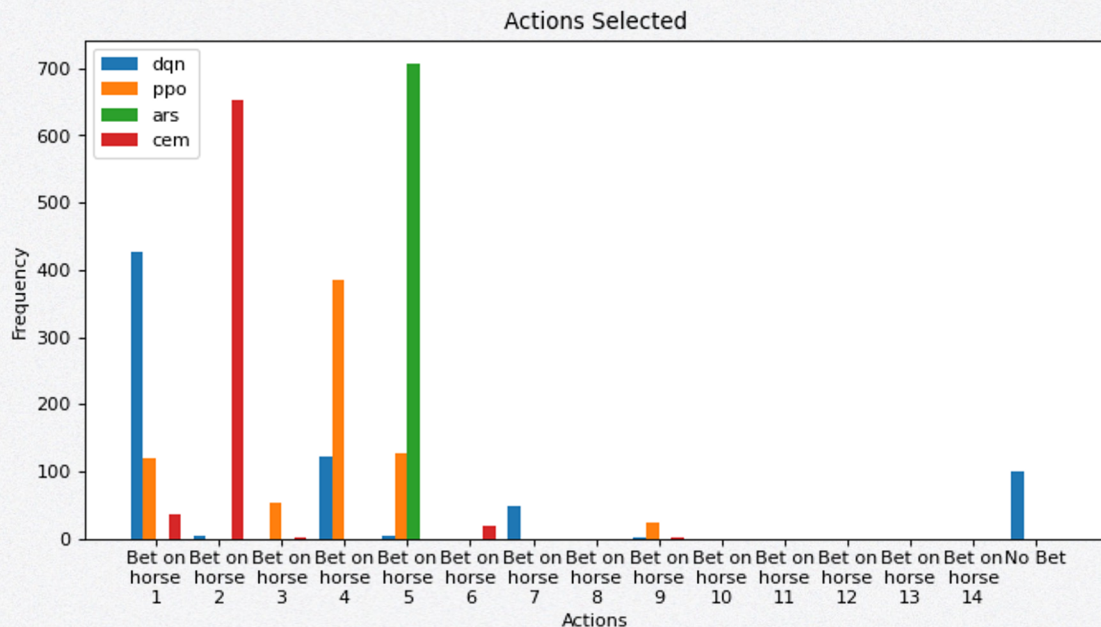
# Win Rate (Type 2)



- **CEM** has **highest** win rate
- **ARS** has **highest** loss rate
- **Majority** of selection are **betting**



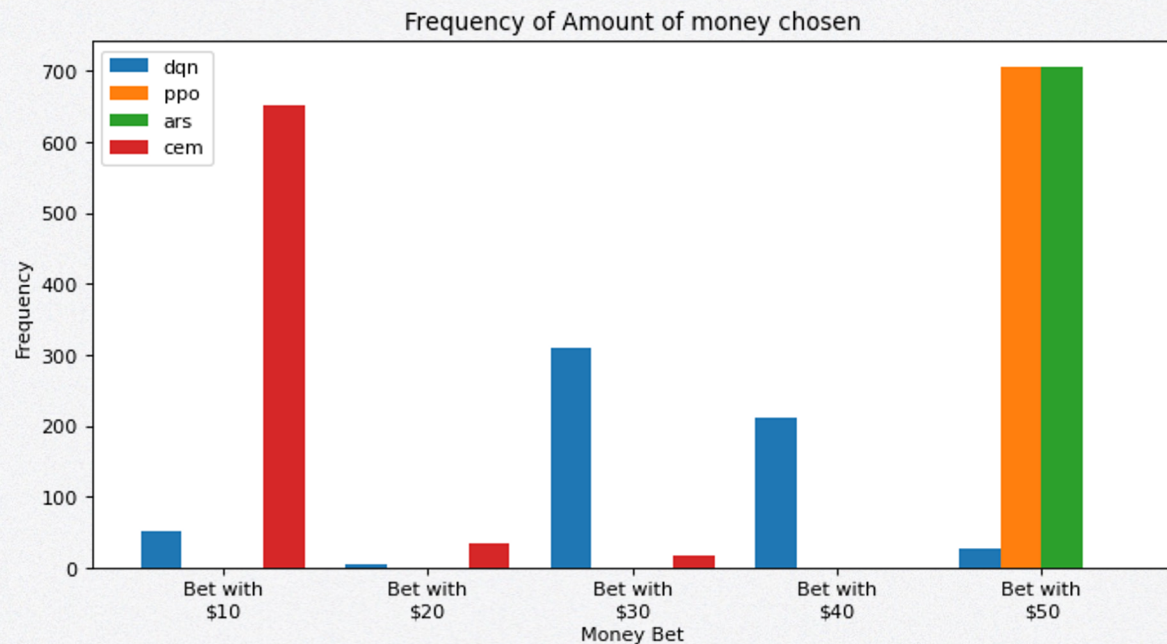
# Actions Selected (Type 2)



- Only **ARS** bet on **single option**
- **DQN, PPO & CEM** bet safer than before



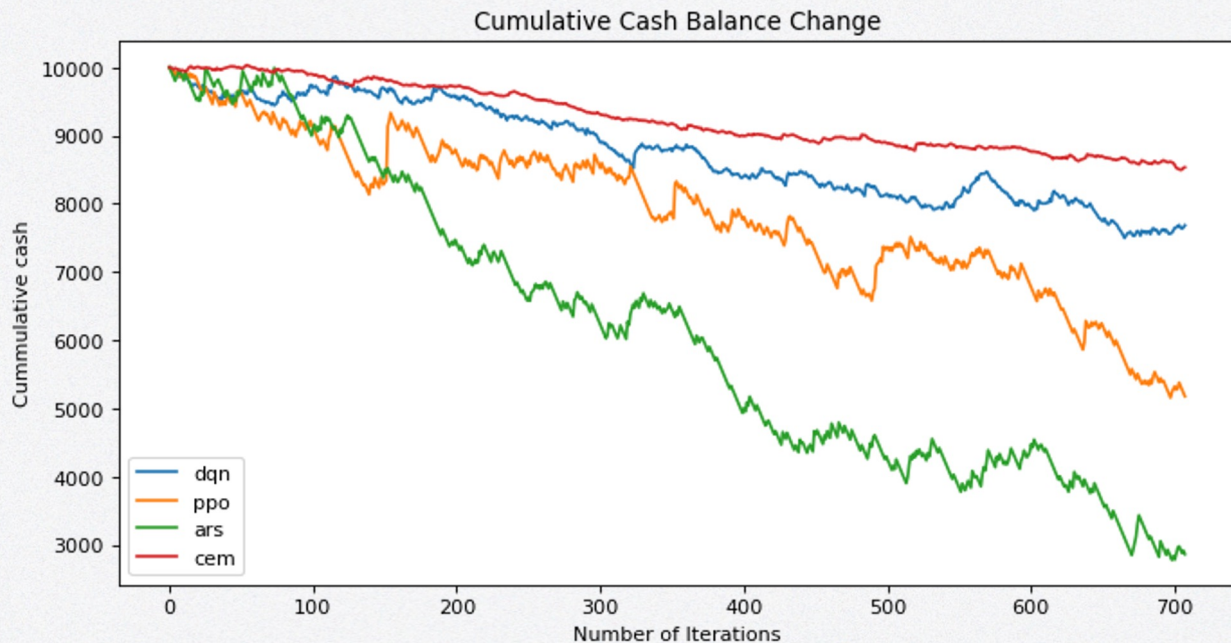
# Money Actions Selected (Type 2)



- PPO & ARS only bet \$50
- CEM mostly bet with \$10
- DQN bets with different amount



# Profitability (Type 2)



- **All losing money**
- **CEM** perform **better** than others
- **PPO & ARS** has great loss





# Overall Comparison



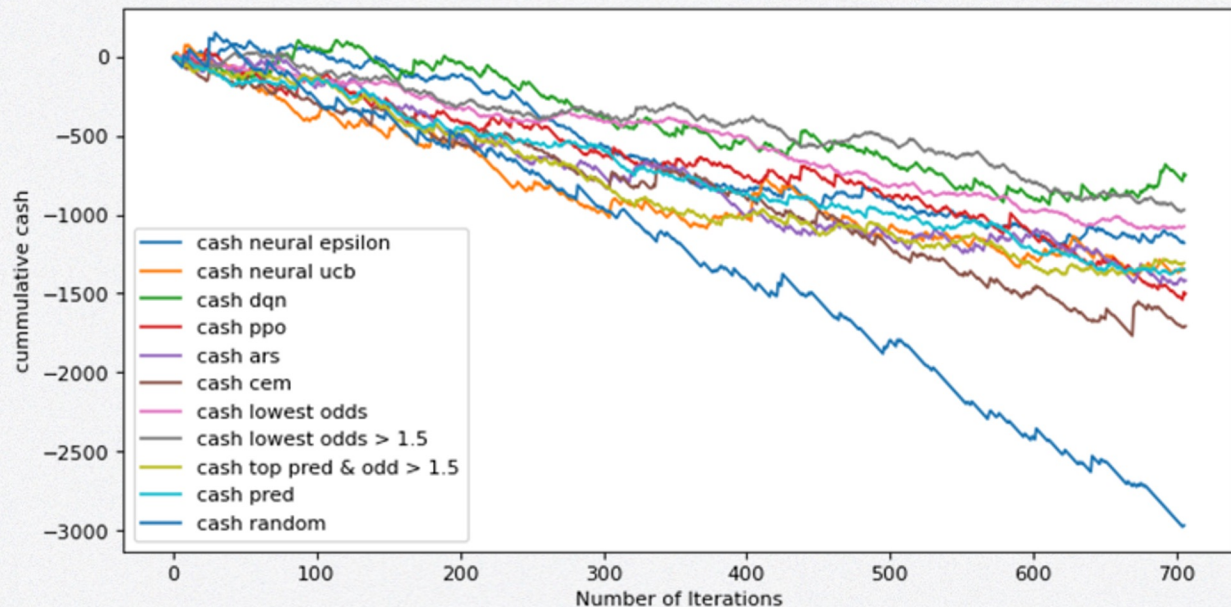
# Optimal Actions Counts

	Optimal	Sub-optimal	Non-optimal
Neural Epsilon	53 (7.50%)	243 (34.37%)	411 (58.13%)
Neural UCB	65 (9.19%)	117 (16.55%)	525 (74.26%)
DQN	59 (8.35%)	205 (29.00%)	443 (62.66%)
PPO	63 (8.91%)	197 (27.86%)	447 (63.22%)
ARS	89 (12.59%)	127 (17.96%)	491 (69.45%)
CEM	59 (8.35%)	84 (11.88%)	564 (79.77%)

- Optimal:
  - Place: **top 3**
  - Reward: **top 3**
- Sub-optimal:
  - Place: **top 3**
- Non-optimal:
  - otherwise




# Overall Comparison (Bet 1 option)



- **Lowest odd > 1.5** outperform other
- **DQN** perform the best among all algorithms





# Model Selection



# Why Model Selection

**Model selection:** selecting best suitable model at each time step

- No guarantee that a particular algorithm consistently performs well
- The best performing algorithm might be different over time
- Combining power of different algorithms

**How?**

We again use bandit algorithm (**EXP3**)



# Why EXP3

**EXP3** (Exponential-weight algorithm for **E**xploration and **E**xploitation)

- Adversarial Bandit (no assumption to make it work)
- Only update belief by reward (we don't use contextual since it would be just trying to approximate other algorithms)
- sensitive to reward changes(exponential)

Suitable when the behavior of algorithms might constantly changing



# Procedure

EXP3 picks one algorithm at a time and bet according to the decision of the chosen algorithm

## Action Set

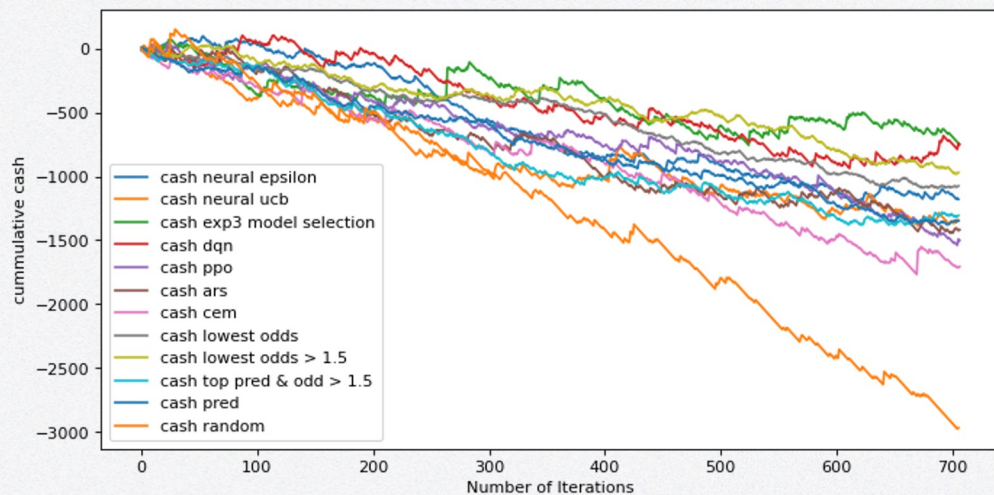
- Algorithms include DQN, PPO, ARS, CEM, neural bandit, neural UCB.
- All run on the simplest setting (bet on 1 horse at a time with \$10 bet)

## Reward

- Reward of selected algorithm by betting on its decided horse



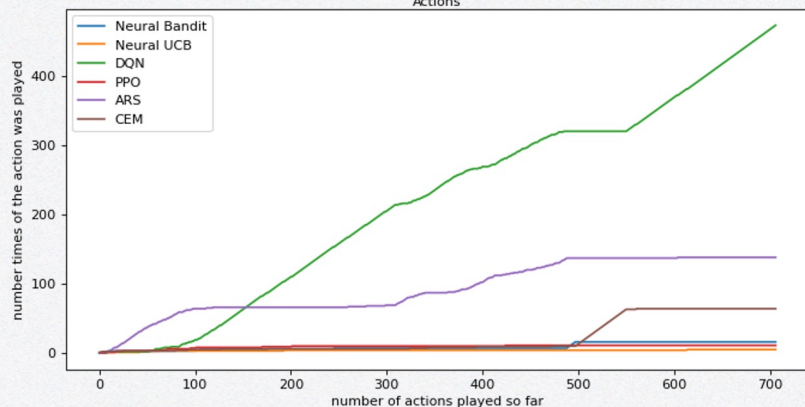
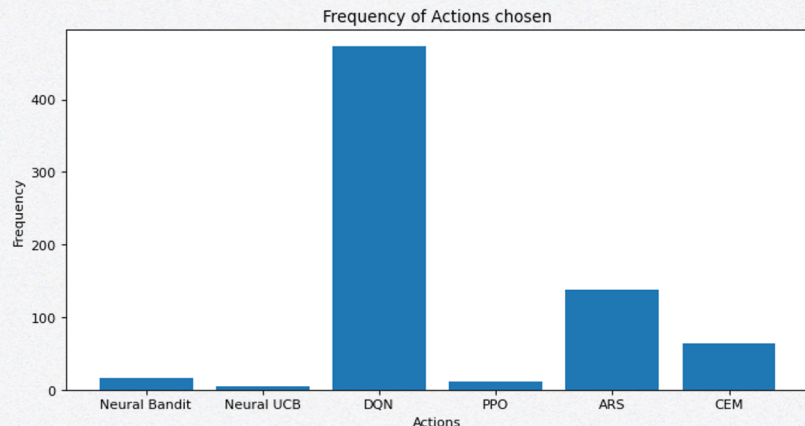
# Result



Using EXP3 to  
do model selection  
**outperforms** any single  
algorithm!



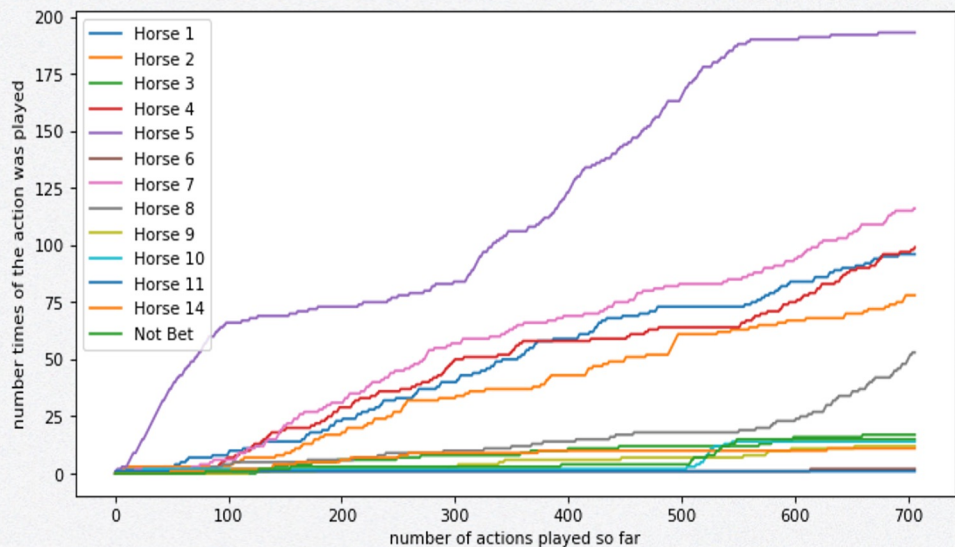
# Comparing algorithms by EXP3



- DQN most selected overtime and follow by ARS and CEM
- Bandit is less selected which shows its weaker performance compared to others



# Observing betting strategy from EXP3



- Horse 5 is selected the most. And followed by 7, 11, 4, 2
- Not bet is seldomly chosen
- Almost all are not safe options but EXP3 doesn't lose much at the end





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# Conclusion



# Conclusion

- Horse racing prediction model
  - Enhanced interpretability of random forest
    - Showed how features affect the results
  - Acceptable betting strategy
    - Based on error range
    - Reduced loss without missing a lot profits
- Horse betting strategies
  - Bandit algorithms
    - Not flexible (variable bet, unaware of state like cash balance, hardly profit for negative expected return)  
-> better use other algorithms
      - But can be used in other scenarios
      - Shown good performance in model selection
  - Other algorithms
    - Comparable accuracy and profits to the bandits





**6**

# **Q&A Section**





**The End  
Thanks!**