

Detecting Multi-Layer Layout Hotspots with Adaptive Squish Patterns

Haoyu Yang¹, Piyush Pathak², Frank Gennari²,
Ya-Chieh Lai², Bei Yu¹

¹The Chinese University of Hong Kong

²Cadence Design Systems Inc.



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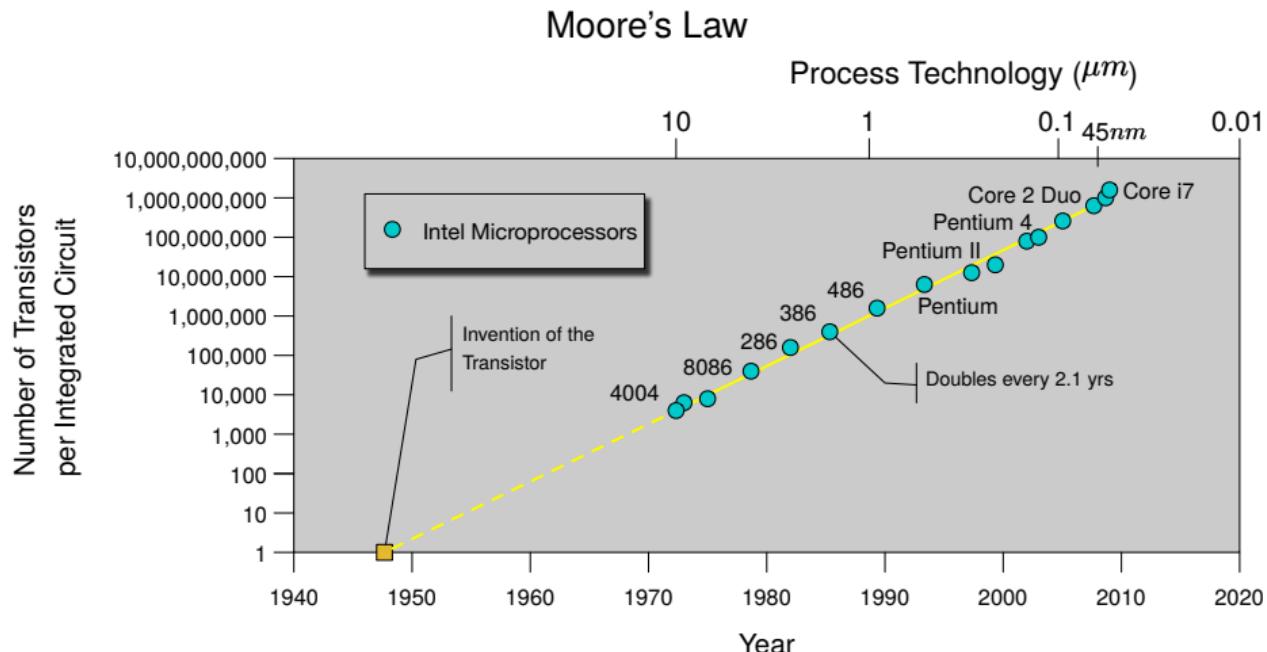
Introduction

The Algorithm

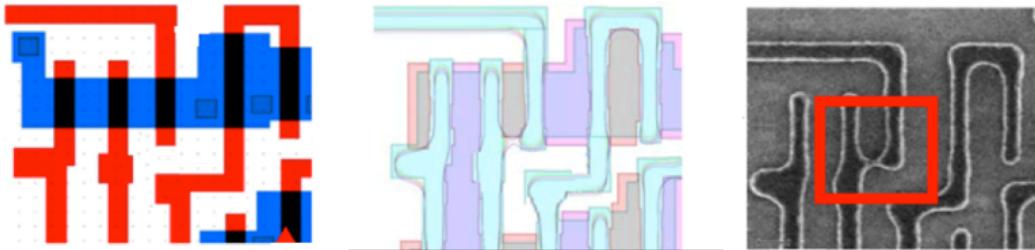
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Moore's Law to Extreme Scaling

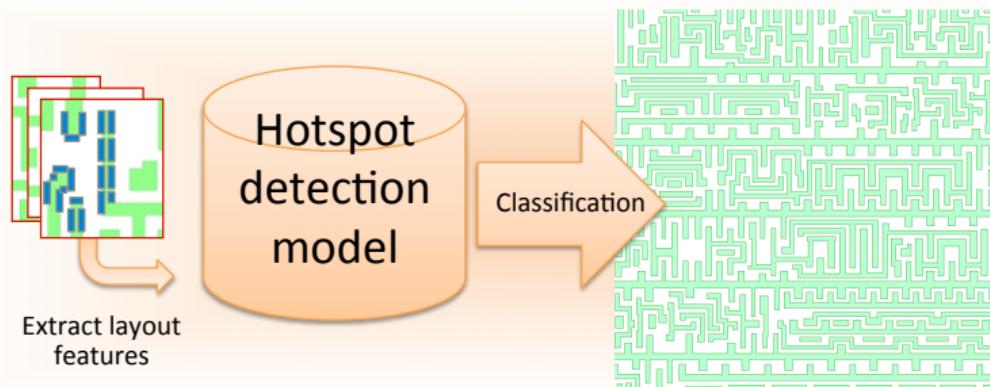


Lithography Proximity Effect

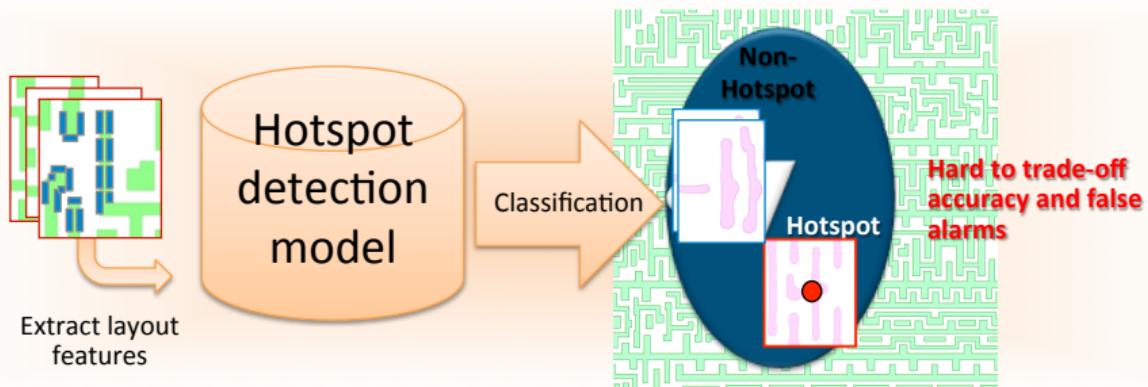


- ▶ What you see \neq what you get
- ▶ Diffraction information loss
- ▶ RET: OPC, SRAF, MPL
- ▶ Worse on designs under 10nm or beyond

Machine Learning based Hotspot Detection

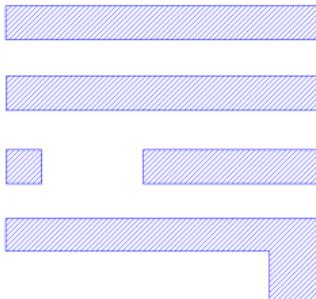


Machine Learning based Hotspot Detection

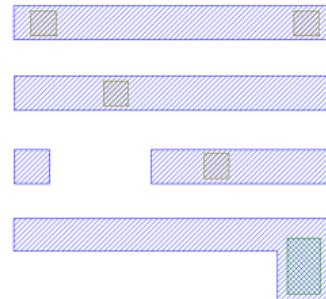


- ▶ Predict new patterns
- ▶ Decision-tree, ANN, SVM, Boosting, Deep Neural Networks
- ▶ [Drmanac+,DAC'09] [Ding+,TCAD'12] [Yu+,JM3'15] [Matsunawa+,SPIE'15]
[Yu+,TCAD'15][Zhang+,ICCAD'16][Yang+,DAC'17][Yang+,TCAD]

Multi-Layer Hotspots



(a)

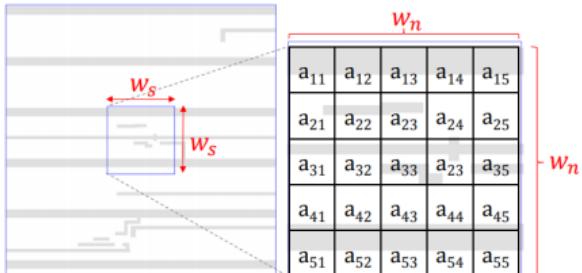


(b)

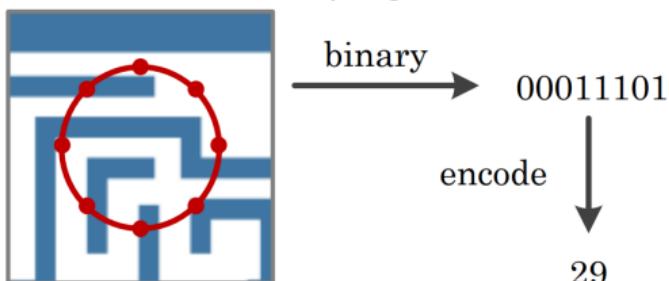
- ▶ More complicated patterns
- ▶ More failure types (e.g. Metal-to-Via failure)

Layout Representations

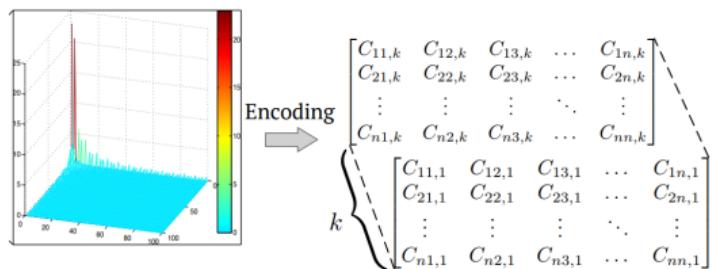
- Density-based features [Matsunawa+, SPIE'15]



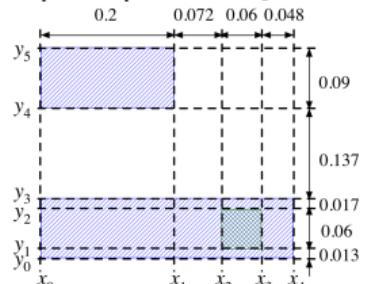
- Concentric circle sampling [Zhang+, ICCAD'16]



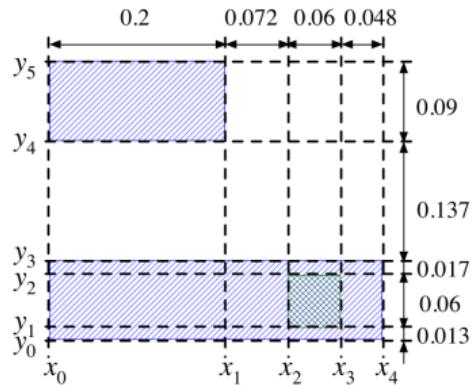
- Feature tensor extraction [Yang+, TCAD]



- Squish patterns [Gennari+, US Patent]



Squish Patterns



A simple multilayer pattern example with scan lines.

- ▶ Lossless
- ▶ Storage-friendly
- ▶ Incompatible with most machine learning engines.
Squish representation does not guarantee a fixed tensor dimensionality for a given clip size.

$$\vec{T} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 3 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix},$$
$$\vec{\delta}_x = [0.2 \quad 0.072 \quad 0.06 \quad 0.048],$$
$$\vec{\delta}_y = [0.013 \quad 0.06 \quad 0.017 \quad 0.137 \quad 0.09].$$

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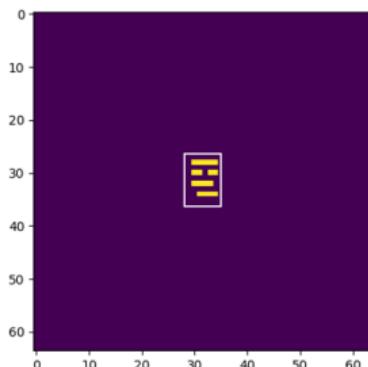
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An Alternative of Padding

- ▶ Legacy padding induces large fraction of zeros that are not informative to CNNs.
- ▶ Instead of padding, we repeat certain rows or columns of squish topologies.
- ▶ $\vec{\delta}$ s are adjusted accordingly to make the pattern unchanged.



$$\vec{T} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 3 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}, \vec{T}' = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 3 & 1 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix}.$$

Which Rows/Columns Are to Be Duplicated/Repeated?

- ▶ In machine learning, if some entries of the input are too large/small, there will be bias related to those entries.
- ▶ Subtract RGB means in conventional image classification tasks.
- ▶ Duplicate rows/columns with larger deltas.

Adaptive Squish Problem:

$$\min_{\vec{s}} \|\vec{\delta}'\|_{\infty} \quad (1a)$$

$$\text{s.t. } \delta'_i = \delta_i / s_i, \forall i, \quad (1b)$$

$$s_i \in \mathbb{Z}^+, \forall i, \quad (1c)$$

$$\sum_i s_i = d. \quad (1d)$$

Repeat Elements

RepeatElements: $\vec{M}' = \text{RepeatElements}(\vec{M}, \vec{s}, a)$, which duplicates the columns ($a = 0$) or rows ($a = 1$) of a matrix $\vec{M} \in \mathbb{R}^{a_1 \times a_2}$ by certain times such that the shape of the new matrix \vec{M}' will be increased to a desired value.

- ▶ $a = 0 :$

$$\vec{m}'_k = \vec{m}_j, \forall \sum_{i=1}^{j-1} s_i < k \leq \sum_{i=1}^j s_i. \quad (2)$$

- ▶ $a = 1 :$

$$\text{RepeatElements}(\vec{M}, \vec{s}, 1) = \text{RepeatElements}(\vec{M}^\top, \vec{s}, 0)^\top. \quad (3)$$

Repeat Elements

For example, if we let $\vec{s} = [1 \ 1 \ 2 \ 1]^\top$ and $a = 0$, then the RepeatElements operation on the topology matrix \vec{T} will result in

$$\vec{T} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 3 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} \rightarrow \vec{T}' = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 3 & 3 & 1 \\ 1 & 1 & 1 & 1 & 1 \end{bmatrix}. \quad (4)$$

Adaptive Squish: Solution 1

- Extend a 3×3 squish topology to shape 3×6 .

Algorithm 1 Obtaining adaptive squish patterns with a greedy procedure.

Input: T, δ, a, d_0, d ;

Output: T, δ ;

```
1: while  $d_0 < d$  do
2:    $s \leftarrow \mathbf{1} \in \mathbb{R}^{d_0}$ ,  $i \leftarrow \arg \max_i \{\delta_i | i = 1, 2, \dots, d_0 - 1\}$ ;
3:    $s_i \leftarrow 2$ ,  $\delta_i \leftarrow \delta_i / 2, \forall i$ ;
4:    $\delta \leftarrow \text{RepeatElements}(\delta, s, 1)$ ;
5:    $T \leftarrow \text{RepeatElements}(T, s, a)$ ;
6:    $d_0 \leftarrow d_0 + 1$ ;
7: end while
```

$$\vec{T} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix},$$

$$\vec{\delta}_x = [28 \quad 18 \quad 2], \vec{\delta}_y = [16 \quad 16 \quad 16].$$

$$\vec{T}' = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix},$$

$$\vec{\delta}'_x = [7 \quad 7 \quad 14 \quad 9 \quad 9 \quad 2], \vec{\delta}'_y = [16 \quad 16 \quad 16].$$

Adaptive Squish: Solution 2

Algorithm 2 Deriving an approximate solution of Formula (8) that will be used for generating adaptive squish patterns.

Input: δ, d_0, d ;

Output: s ;

```
1:  $l \leftarrow \sum_i \delta_i$ ;  
2:  $t \leftarrow l/(d - 1)$ ;  
3:  $s_i \leftarrow \max\{1, \text{int}(\delta_i/t)\}, \forall i$ ;  
4: while  $\sum_i s_i < d - 1$  do  
5:    $\delta'_i \leftarrow \delta_i/s_i, \forall i$ ;  
6:    $i \leftarrow \arg \max_i \{\delta_i | i = 1, 2, \dots, d_0 - 1\}$ ;  
7:    $s_i \leftarrow s_i + 1$ ;  
8: end while  
9:  $\delta_i \leftarrow \delta_i/s_i, \forall i$ ;  
10:  $\boldsymbol{\delta} \leftarrow \text{RepeatElements}(\boldsymbol{\delta}, s, 1)$ ;  
11:  $T \leftarrow \text{RepeatElements}(T, s, a)$ ;
```

- Extend a 3×3 squish topology to shape 3×6 .

$$\vec{T} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix},$$

$$\vec{\delta}_x = [28 \quad 18 \quad 2], \vec{\delta}_y = [16 \quad 16 \quad 16].$$

$$\vec{T}' = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix},$$

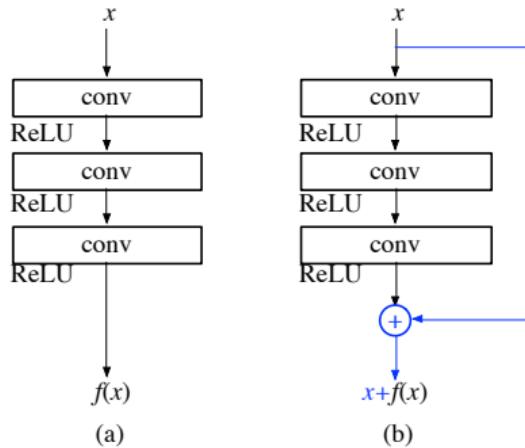
$$\vec{\delta}'_x = [9.33 \quad 9.33 \quad 9.33 \quad 9 \quad 9 \quad 2], \vec{\delta}'_y = [16 \quad 16 \quad 16].$$

Adaptive Squish: Data Preparation

- The squish topology and $\vec{\delta}$ s will be stacked together into a 3D tensor $[\vec{T}'; \vec{\delta}_X'; \vec{\delta}_Y']$ that will be fed into neural networks for training and inference, where,

$$\vec{T}' = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 1 & 1 \end{bmatrix},$$
$$\vec{\delta}_X' = \begin{bmatrix} 9.33 & 9.33 & 9.33 & 9 & 9 & 2 \\ 9.33 & 9.33 & 9.33 & 9 & 9 & 2 \\ 9.33 & 9.33 & 9.33 & 9 & 9 & 2 \end{bmatrix},$$
$$\vec{\delta}_Y' = \begin{bmatrix} 16 & 16 & 16 & 16 & 16 \\ 16 & 16 & 16 & 16 & 16 \\ 16 & 16 & 16 & 16 & 16 \end{bmatrix}.$$

ResNet Block



- ▶ Gradient vanishing problem.
- ▶ Allows gradient to be easily backpropagated to early layers.
- ▶ Feature reuse.

The Neural Network Architecture

JM3 [Yang+, JM3'17]					Ours				
Layer	Filter	Stride	Output	Parameter	Layer	Filter	Stride	Output	Parameter
conv1-1	$3 \times 3 \times 4$	2	$160 \times 160 \times 4$	36	conv1-1	$5 \times 5 \times 128$	2	$32 \times 32 \times 128$	9600
conv1-2	$3 \times 3 \times 4$	2	$80 \times 80 \times 4$	144	conv1-2	$5 \times 5 \times 128$	1	$32 \times 32 \times 128$	409600
conv2-1	$3 \times 3 \times 8$	1	$80 \times 80 \times 8$	288	conv1-3	$5 \times 5 \times 128$	1	$32 \times 32 \times 128$	409600
conv2-2	$3 \times 3 \times 8$	1	$80 \times 80 \times 8$	576	conv1-4	$5 \times 5 \times 128$	1	$32 \times 32 \times 128$	409600
conv2-3	$3 \times 3 \times 8$	1	$80 \times 80 \times 8$	576	conv2-1	$5 \times 5 \times 256$	2	$16 \times 16 \times 256$	819200
pool2	2×2	2	$40 \times 40 \times 8$		conv2-2	$5 \times 5 \times 256$	1	$16 \times 16 \times 256$	1638400
conv3-1	$3 \times 3 \times 16$	1	$40 \times 40 \times 16$	1152	conv2-3	$5 \times 5 \times 256$	1	$16 \times 16 \times 256$	1638400
conv3-2	$3 \times 3 \times 16$	1	$40 \times 40 \times 16$	2304	conv2-4	$5 \times 5 \times 256$	1	$16 \times 16 \times 256$	1638400
conv3-3	$3 \times 3 \times 16$	1	$40 \times 40 \times 16$	2304	conv3-1	$5 \times 5 \times 512$	2	$8 \times 8 \times 512$	3276800
pool3	2×2	2	$20 \times 20 \times 16$		conv3-2	$5 \times 5 \times 512$	1	$8 \times 8 \times 512$	6553600
conv4-1	$3 \times 3 \times 32$	1	$20 \times 20 \times 32$	4608	conv3-3	$5 \times 5 \times 512$	1	$8 \times 8 \times 512$	6553600
conv4-2	$3 \times 3 \times 32$	1	$20 \times 20 \times 32$	9216	conv3-4	$5 \times 5 \times 512$	1	$8 \times 8 \times 512$	6553600
conv4-3	$3 \times 3 \times 32$	1	$20 \times 20 \times 32$	9216	conv4-1	$5 \times 5 \times 1024$	2	$4 \times 4 \times 1024$	13107200
pool4	2×2	2	$10 \times 10 \times 32$						
conv5-1	$3 \times 3 \times 32$	1	$10 \times 10 \times 32$	9216					
conv5-2	$3 \times 3 \times 32$	1	$10 \times 10 \times 32$	9216					
conv5-3	$3 \times 3 \times 32$	1	$10 \times 10 \times 32$	9216					
pool5	2×2	2	$5 \times 5 \times 32$						
fc1			2048	1638400	fc1			1024	16777216
fc2			512	1048576	fc2			2	2048
fc3			2	1024					
Summary			2746068					59796864	

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The Dataset & Configurations

- ▶ 14nm metal layer, M3, V3, V4

	Train	Test	Image	Squish
Hotspot	3073	6015	320×320	$64 \times 64 \times 3$
Nonhotspot	973197	1457830		

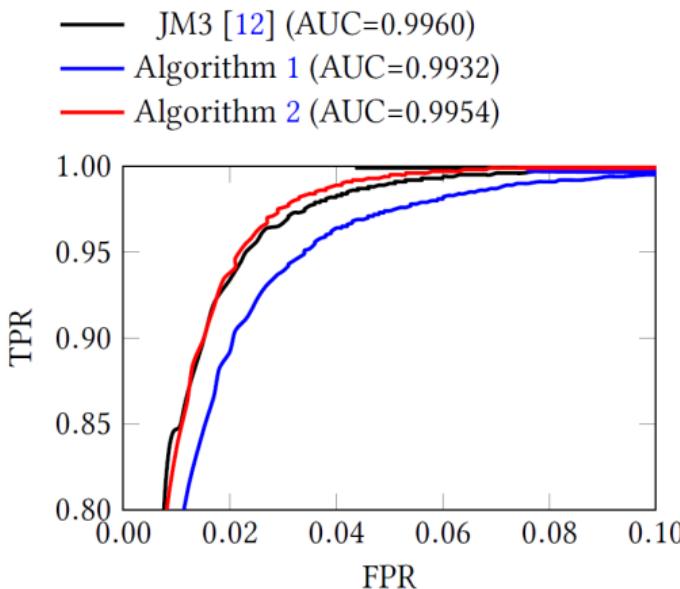
- ▶ Initial learning rate: 0.001
- ▶ Decay: 0.7 per 2000 steps
- ▶ Weight normalization: 0.001
- ▶ Xavier, Adam

Results

- ▶ Hit : # of hotspot patterns that are predicted as hotspots
- ▶ False Alarm : # of good patterns that are predicted as hotspots

Item	JM3 [Yang+,JM3'17]	Algorithm 1	Algorithm 2
Accuracy (%)	98.87	97.51	99.24
False Alarm Rate (%)	4.81	5.05	4.52
Hit	5947	5865	5969
False Alarm	70193	73645	65926
Precision (%)	7.81	7.38	8.30

Receiver Operating Characteristics



- ▶ JM3 behaves even better than Algorithm 2 in terms of area under curve.
- ▶ AUC advantages of JM3 comes from the region where the decision threshold is above 0.9.
- ▶ Higher confidence on hotspot patterns that can be correctly predicted by classifiers is not necessary.

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Conclusion

- ▶ Adaptive Squish Pattern.
Attains good properties of squish patterns and compatible with most learning machines.
- ▶ Multilayer Hotspot Detection.
First time consider metal-to-via failure.
- ▶ ResNet.
Allow better convergence and model generality.