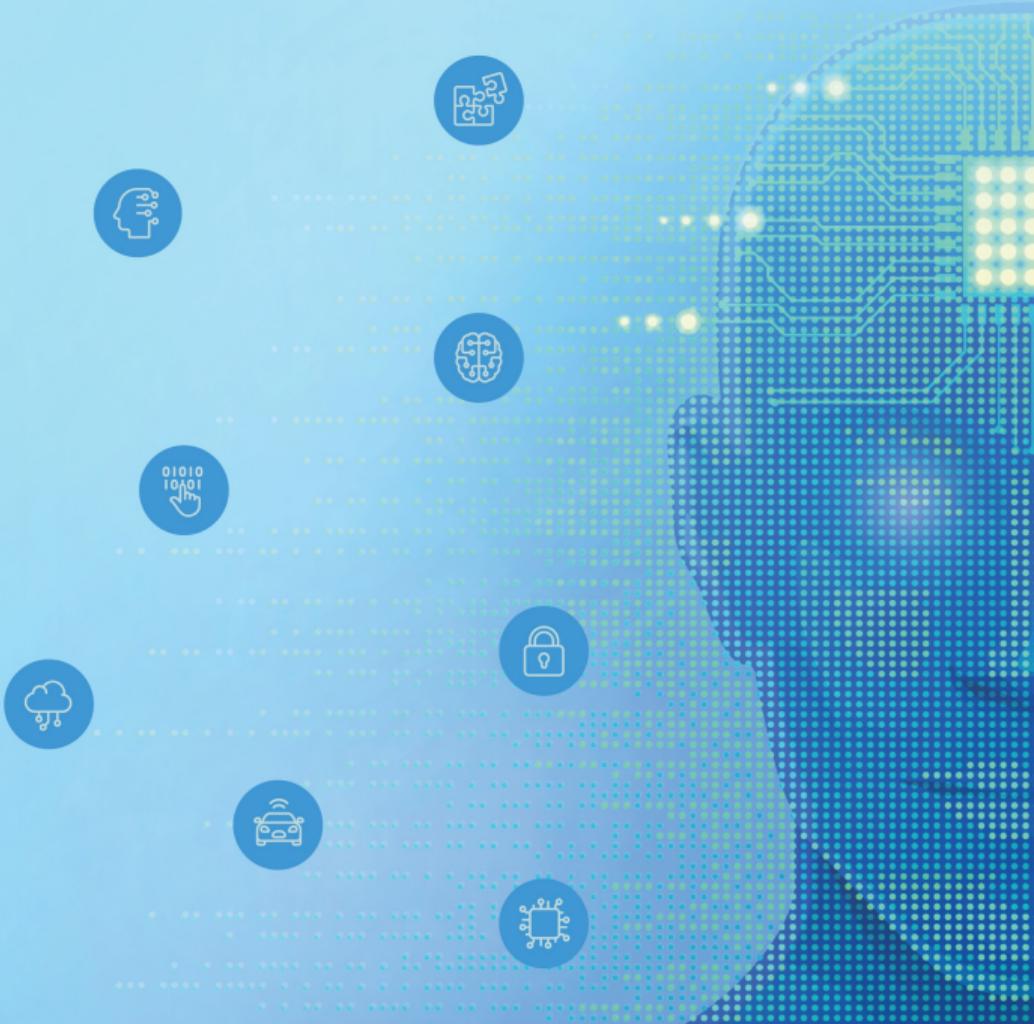




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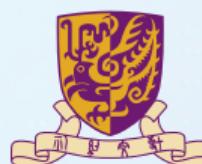


# Concurrent Sign-off Timing Optimization via Deep Steiner Points Refinement

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# Outline

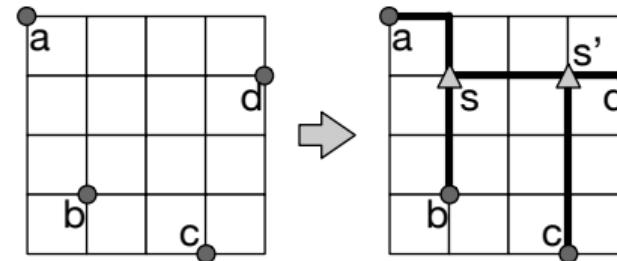
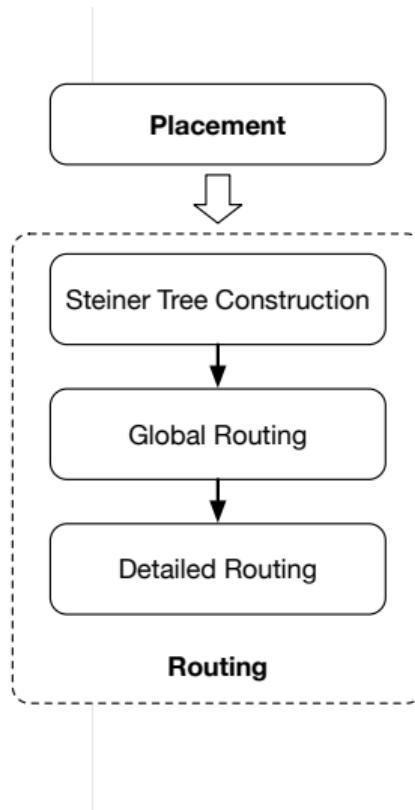
1 Introduction

2 TSteiner

3 Results

4 Conclusion

# Physical Design



Steiner tree construction

- Modern routing stage includes three stages.
- Steiner tree decomposes the multi-pin net into a set of two-pin net.

# Early Stage Timing Optimization

- Placement<sup>1 2</sup>: Pre-routing timing metrics.
- Routing<sup>3 4 5 6</sup>: Path lengths, early timing metrics.

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<sup>1</sup>P. Liao, and et al., "DREAMPlace 4.0: timing-driven global placement with momentum-based net weighting," DATE 2022

<sup>2</sup>Z. Guo and Y. Lin, "Differentiable-Timing-Driven Global Placement," DAC 2022

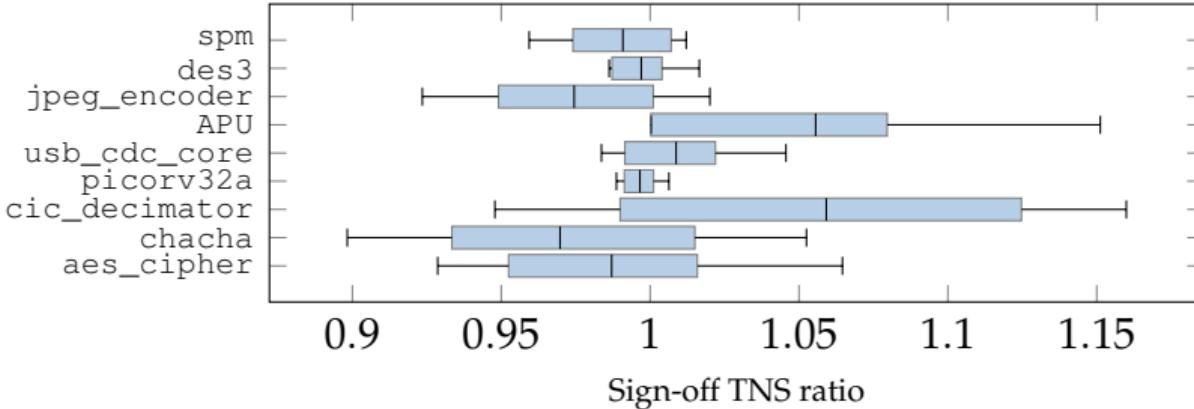
<sup>3</sup>C. J. Alpert, and et al., "Timing-driven Steiner trees are (practically) free," DAC 2006

<sup>4</sup>C. J. Alpert, and et al., "Prim-Dijkstra revisited: Achieving superior timing-driven routing trees," ISPD 2018

<sup>5</sup>S. Held, and et al., "Global routing with timing constraints," TCAD 2017

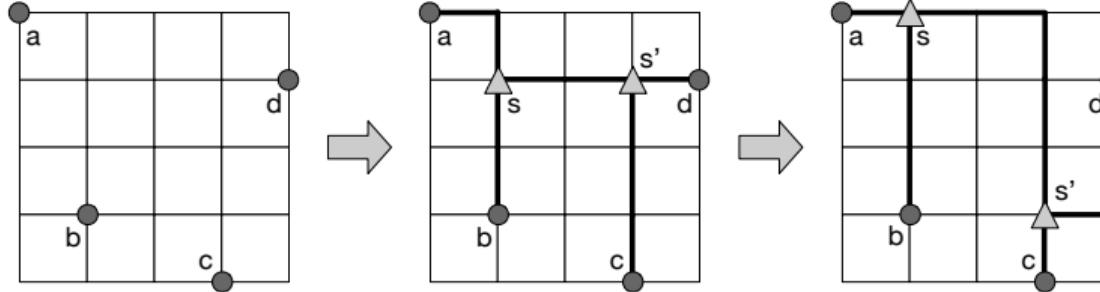
<sup>6</sup>D. Wu, and et al., "Timing driven track routing considering coupling capacitance," ASPDAC 2005

# Random Steiner Point Disturbance



- The sign-off timing performance could be significantly affected even by a random disturbance on Steiner point position.
- The impact of random moving is considerably unstable, and its average performance is slight.

# Steiner Point Refinement

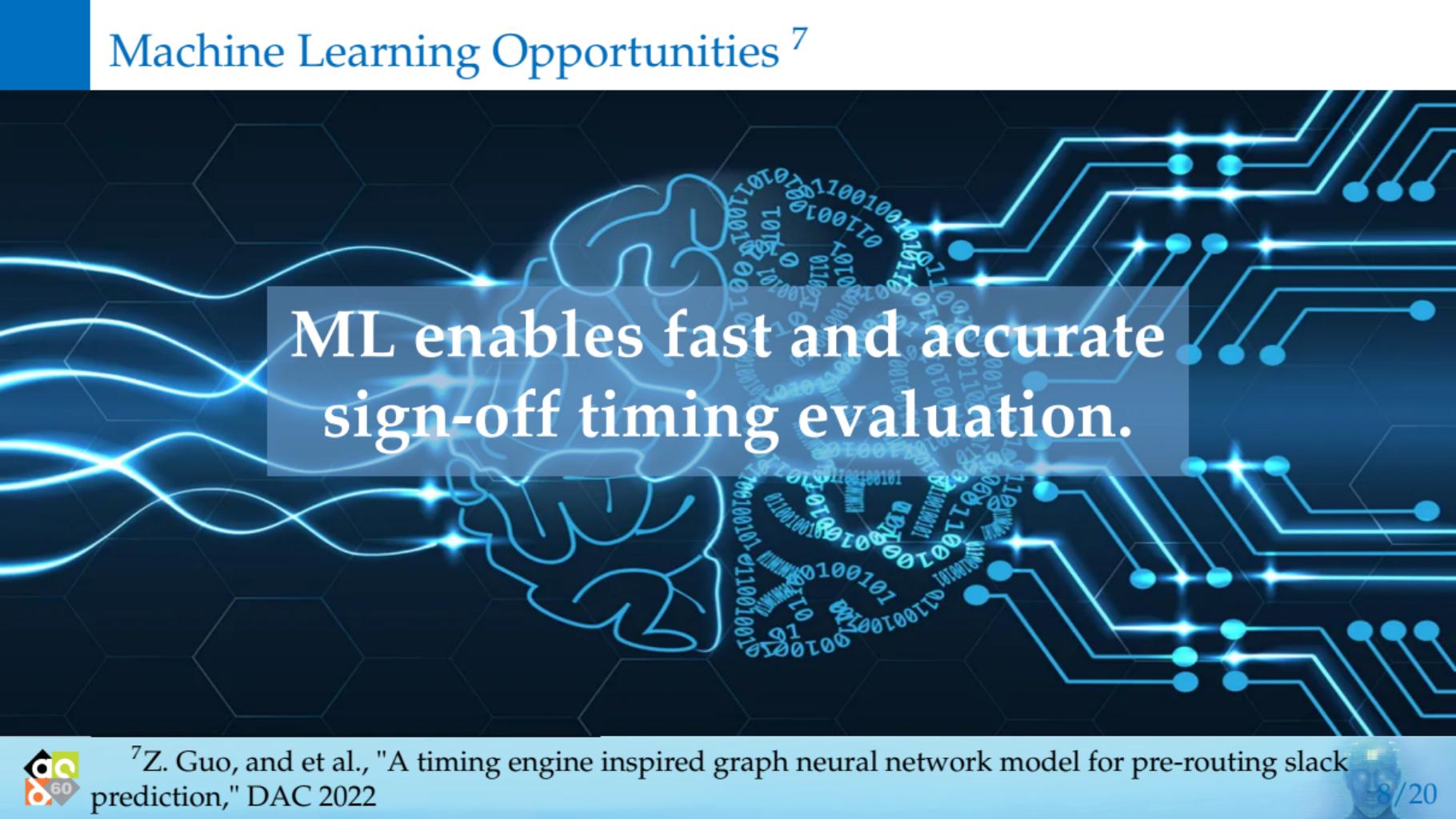


Steiner point refinement

## Timing-driven Steiner Point Refinement

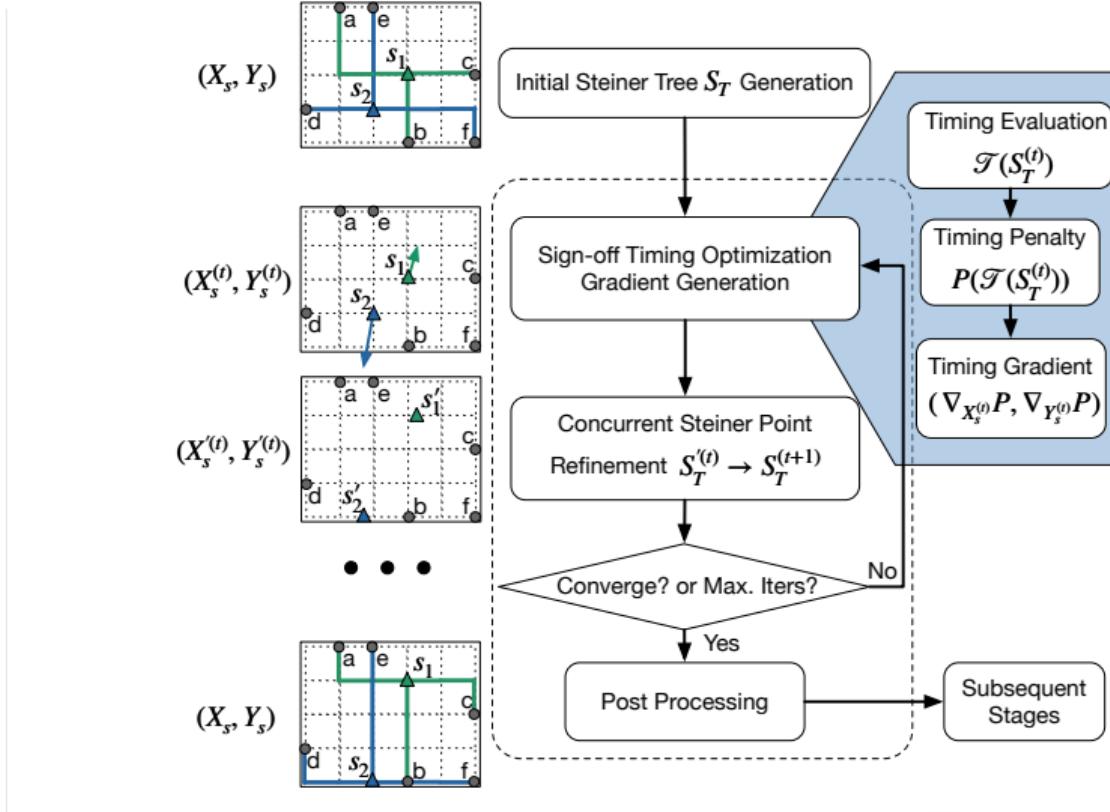
Given an initial Steiner tree set  $S_T = \{T^1, T^2, \dots, T^n\}$ ,  $T^i = (V_c^i, V_s^i, E^i)$ , where  $V_c^i$  is the set of cell nodes,  $V_s^i$  is the set of Steiner nodes and  $E^i$  means the edges connecting  $V_c^i$  and  $V_s^i$  of the  $i^{\text{th}}$  Steiner tree, our task is to refine the position  $(X_s, Y_s)$  of  $V_s = \{V_s^i, 1 \leq i \leq n\}$  in the pre-routing stage to obtain better **sign-off** timing performance.

# Machine Learning Opportunities<sup>7</sup>



ML enables fast and accurate sign-off timing evaluation.

# Overall flow - TSteiner

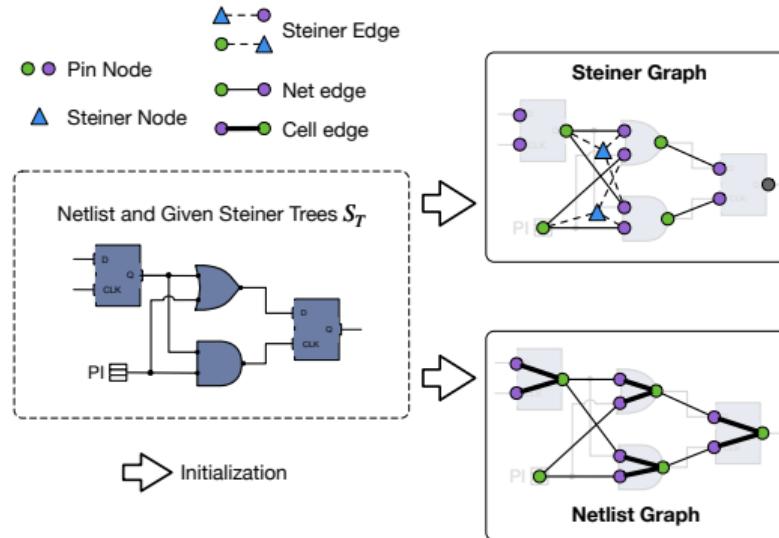


# Sign-off Timing Optimization Gradients

## Sign-off Timing Evaluation

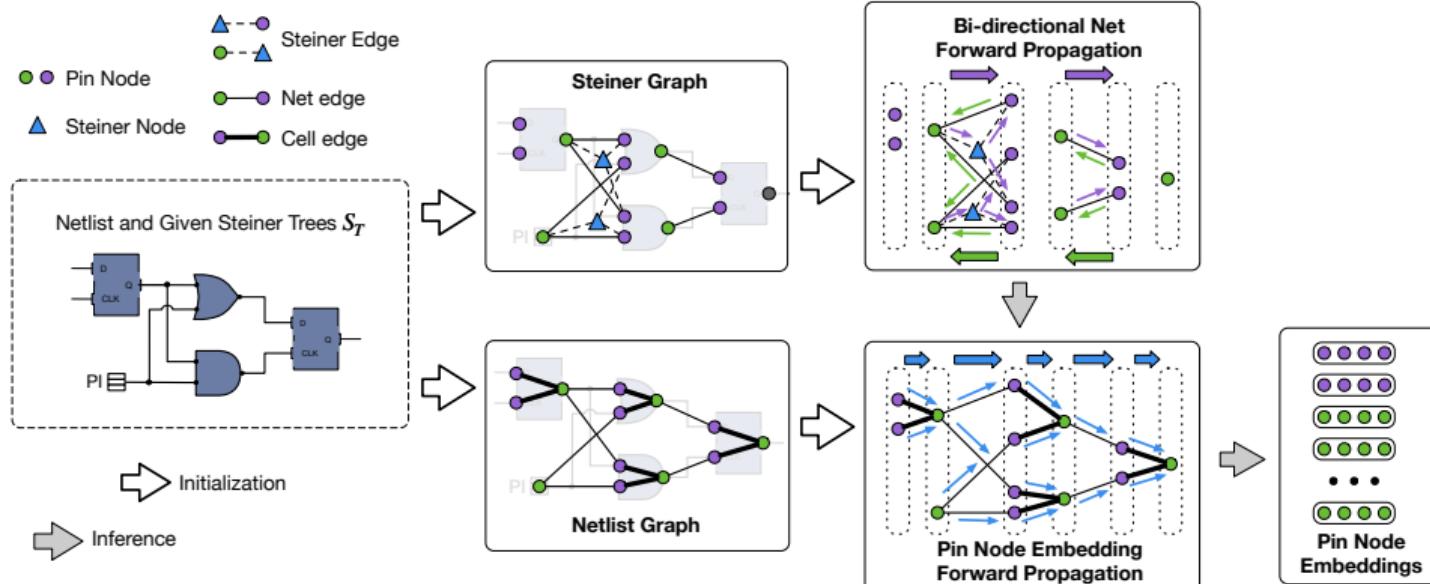
Given a Steiner tree solution  $S_T$ , timing evaluation is to find an estimator  $\mathcal{T}$  to evaluate the sign-off timing metrics  $\mathcal{T}(S_T)$ , i.e., arrival time at each pin.

# Sign-off Timing Optimization Gradients - Initialization



- **Steiner Graph:** pin node and Steiner node; net edge and Steiner edge.
- **Netlist Graph:** pin node; cell edge and net edge.

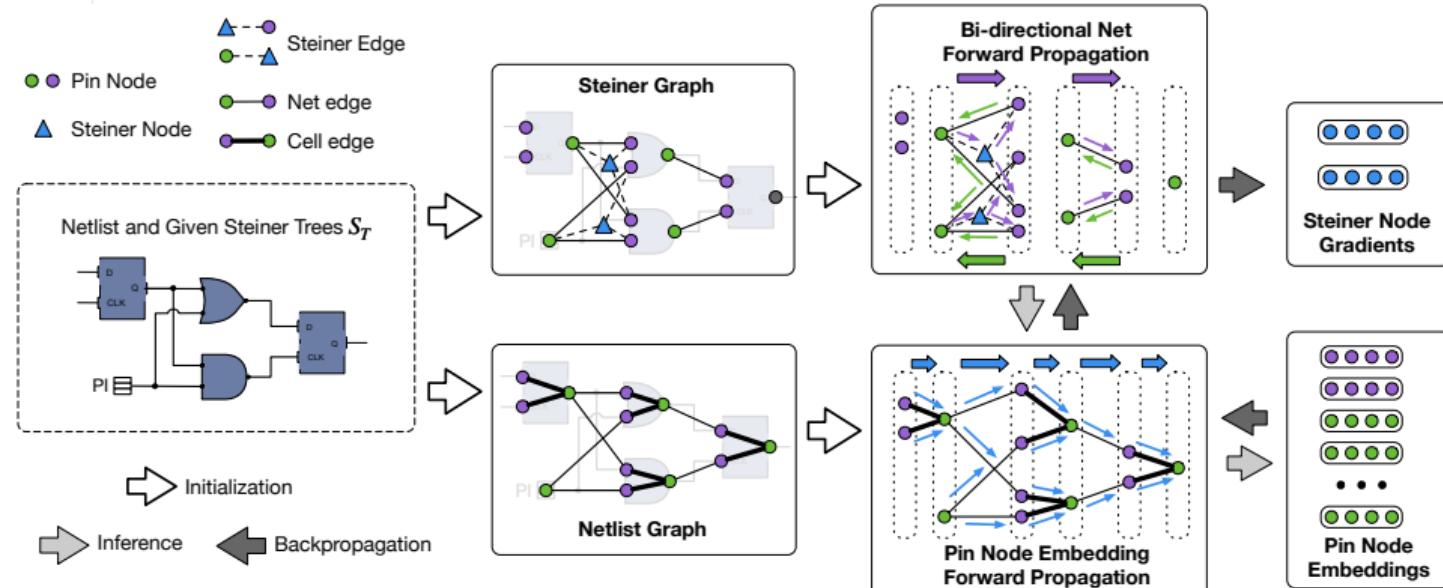
# Sign-off Timing Optimization Gradients - Inference



The timing penalty can be calculated with,

$$P(\mathcal{T}(S_T)) = \lambda_w w(\mathcal{T}(S_T)) + \lambda_t t(\mathcal{T}(S_T)). \quad (1)$$

# Sign-off Timing Optimization Gradients - Backpropagation



- The timing optimization gradients w.r.t. Steiner points positions ( $\nabla_{X_s} P, \nabla_{Y_s} P$ ) can be computed automatically via backward propagation.

# Concurrent timing-driven Steiner Point Refinement

## Adam Stochastic Optimizer

$$\begin{aligned} m_x^{(t)} &= (1 - \beta_1) \cdot \nabla_{X_s^{(t)}} P, \quad v_x^{(t)} = (1 - \beta_2) \cdot (\nabla_{X_s^{(t)}} P \odot \nabla_{X_s^{(t)}} P), \\ X_s'^{(t)} &= X_s^{(t)} - \theta \cdot \frac{m_x^{(t)}}{\sqrt{v_x^{(t)}} + \epsilon}, \end{aligned} \tag{2}$$

where  $\theta$  is the stepsize to optimize Steiner point positions;  $\beta_1$ ,  $\beta_2$ , and  $\epsilon$  are the hyper-parameters.

## Adaptive Stepsize Scheme - *Adaptive\_Theta*

- ① Obtain the initial timing gradient  $(\nabla_{X_s} P, \nabla_{Y_s} P)$  w.r.t. the given Steiner point positions  $(X_s, Y_s)$ .
- ② Apply a small move:

$$\begin{aligned} X'_s &= X_s + \alpha \nabla_{X_s} P, \\ Y'_s &= Y_s + \alpha \nabla_{Y_s} P, \end{aligned} \tag{3}$$

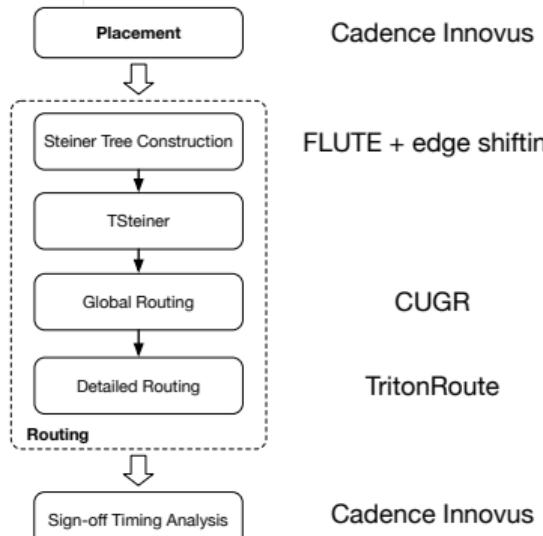
where  $\alpha$  is a hyper-parameter to control the scale of  $\theta$ .

- ③ Obtain the updated timing gradient  $(\nabla_{X'_s} P, \nabla_{Y'_s} P)$ .

The adaptive stepsize is then calculated as:

$$\theta = \frac{|(X_s, Y_s) - (X'_s, Y'_s)|_2}{|(\nabla_{X_s} P, \nabla_{Y_s} P) - (\nabla_{X'_s} P, \nabla_{Y'_s} P)|_2}. \tag{4}$$

# Setting



Cadence Innovus

FLUTE + edge shifting

CUGR

TritonRoute

Cadence Innovus

Table: Benchmark statistics.

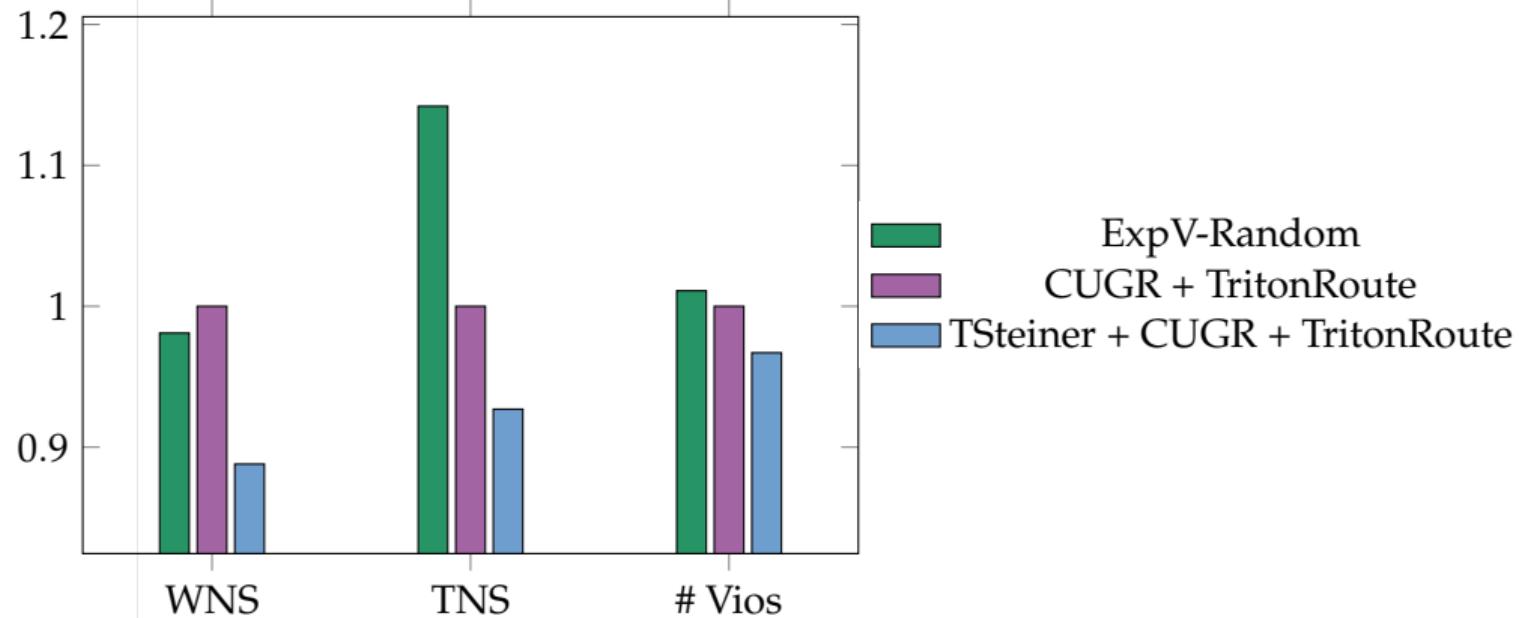
Benchmark	# Nodes		# Edges		# Endpoints
	Cell	Steiner	Net	Cell	
chacha	15700	5398	44468	41204	1972
cic_decimator	781	196	2112	1982	130
APU	2897	1154	8373	7918	427
des	14652	5487	43065	40432	2048
jpeg_encoder	55264	15982	170520	161743	4420
spm	238	63	645	516	129
aes_cipher	11532	7323	37085	35825	659
picorv32a	13622	4542	41030	38191	1879
usb_cdc_core	1642	625	4632	3999	626
des3	47410	20004	136257	125093	8872
Total Train	89532	28280	269183	253795	9126
Total Test	74206	32494	219004	203108	12036

# Results

**Table:** Experimental results on real-world open-source designs compared to the routing flow without integrating TSteiner.

Benchmark	CUGR + TritonRoute						TSteiner + CUGR + TritonRoute					
	WNS (ns)	TNS (ns)	# Vios	WL( $\times 10^6$ )	# Vias	# DRV	WNS (ns)	TNS (ns)	# Vios	WL( $\times 10^6$ )	# Vias	# DRV
aes_cipher	-11.246	-1516.9	512	984.971	109574	5	<b>-8.38</b>	<b>-1434.2</b>	<b>504</b>	984.527	109443	3
chacha	-48.538	-26259.1	1378	1,257.427	126600	2	<b>-46.68</b>	<b>-25375.7</b>	<b>1372</b>	1,258.011	126898	2
cic_decimator	-2.834	-169.981	72	16.466	5586	3	<b>-2.724</b>	<b>-161.436</b>	<b>72</b>	16.413	5593	3
picorv32a	-17.762	-441.607	67	727.216	109293	38	<b>-17.686</b>	<b>-434.443</b>	<b>56</b>	727.472	109311	37
usb_cdc_core	-5.914	-1365.2	347	49.351	12396	0	<b>-5.823</b>	<b>-1343.1</b>	<b>346</b>	49.117	12407	0
APU	-2.265	-33.713	25	101.179	23031	3	<b>-2.221</b>	<b>-33.598</b>	<b>25</b>	101.454	23101	3
des	-7.352	-405.427	341	682.828	115698	5	<b>-3.987</b>	<b>-227.331</b>	<b>285</b>	682.788	115599	5
jpeg_encoder	-74.342	-64909.2	<b>1967</b>	2,969.654	439126	1	<b>-70.629</b>	<b>-60789.1</b>	2007	2,973.304	439561	1
des3	-7.048	-1890	1512	2,680.848	372583	<b>48</b>	<b>-5.668</b>	<b>-1879.6</b>	<b>1509</b>	2,684.367	372768	49
spm	-0.817	-65.866	126	4.394	1553	2	<b>-0.782</b>	<b>-63.846</b>	126	4.399	1544	2
Average	1.000	1.000	1.000	1.0000	<b>1.0000</b>	1.0000	<b>0.888</b>	<b>0.929</b>	<b>0.967</b>	<b>0.9999</b>	1.0001	<b>0.9549</b>

# Results



# Conclusion

- We propose a deep learning-assist concurrent early-stage sign-off timing optimization framework, TSteiner.
- This study has raised the importance of Steiner point refinement for timing closure and provides a novel solution for early-stage timing optimization.
- TSteiner can be extended to more physical design stages since Steiner points exist not only in the pre-routing stage but also in routing solutions.
- The connections and the number of Steiner points may limit the optimization performance. => Search for new opportunities to support the flexibility.



# THANK YOU!

