Exercises: Line Integrals by Arc Length

Problem 1. Let C be the curve from point p(0,0) to point q(1,1) on the parabola $y = x^2$. Calculate $\int_C x \, ds$.

Problem 2. Let C be the line segment from point p(1,2,3) to point q(8,7,6). Calculate $\int_C x+z^2 ds$.

Problem 3. Let C be the circle $x^2 + y^2 = 1$. Calculate $\int_C y \, ds$.

Problem 4. Let C be the boundary of the square shown below:



Calculate $\int_C y\,ds.$

Problem 5. Let C be the intersection of two surfaces: sphere $x^2 + y^2 + z^2 = 3$ and plane x = y. Calculate $\int_C x^2 ds$.