

**MATH 2050A - HW 8**

**Due Date:** 26 Nov 2020, 23:59

*You are reminded that your HW is graded  
based on **both** your idea and your presentation*

**Problems:** P.148: 2,6,7

(3 Questions in total)

**Textbook:** Bartle RG, Sherbert DR(2011). Introduction to Real Analysis, fourth edition, John Wiley Sons,Inc.

We type here all the required problems *for your convenience only*. The presentation of the problems here may be different from the original one but the respective solution should be unaffected.

**1** (P.148 Q2). Let  $f(x) := 1/x^2$ . Show that

- i.  $f$  is uniformly continuous on  $A := [1, \infty)$
- ii.  $f$  is not uniformly continuous on  $B := (0, \infty)$

**2** (P.148 Q6). Let  $A \subset \mathbb{R}$  and  $f, g$  be real-valued uniformly continuous functions defined on  $A$ . Show that if  $f, g$  are bounded on  $A$ , then the product  $fg$  is uniformly continuous on  $A$

**3** (P.148 Q7). Let  $f(x) := x$  and  $g(x) := \sin x$  be defined on  $\mathbb{R}$ . Show that

- i.  $f, g$  are uniformly continuous on  $\mathbb{R}$
- ii. the product  $fg$  is not uniformly continuous on  $\mathbb{R}$