MATH 2060B - HW 2 Due Date: 3 Feb 2021, 23:59

Problems: Ex6.2 P.179: 5, 14; Ex6.4 P.196: 4

(3 Questions in total)

Textbook: Bartle RG, Sherbert DR(2011). Introduction to Real Analysis, fourth edition, John Wiley Sons,Inc.

Instruction:

- 1. Please submit your solution in one pdf file to Blackboard.
- 2. Rename your file in the form "HW1_ChanTaiMan_1155151031".
- 3. You are reminded that your HW is graded based on **both** your idea and your presentation

Questions:

1 (P.179 Q5). Let a > b > 0 and let $n \in \mathbb{N}$ satisfy $n \ge 2$. Show that $a^{1/n} - b^{1/n} < (a - b)^{1/n}$. (If you have spent enough efforts but without progress, you may consult the hint in the footnote¹.)

2 (P.179 Q14). Let *I* be an interval and let $f: I \to \mathbb{R}$ be differentiable on *I*. Suppose f' is never 0 on *I*. Show that either f'(x) > 0 for all $x \in I$ or f'(x) < 0 for all $x \in I$.

3 (P.196 Q4). Let x > 0. Show that

$$1 + \frac{1}{2}x - \frac{1}{8}x^2 \le \sqrt{1 + x} \le 1 + \frac{1}{2}x$$

¹Hint: Consider $f(x) := x^{1/n} - (x-1)^{1/n}$. Show that f is decreasing for $x \ge 1$ and evaluate f at 1 and a/b