## THE CHINESE UNVIERSITY OF HONG KONG Department of Mathematics

## MATH5070 Topology of Manifolds, First term 2022-2023

## Schedule

| Wk | Thursday<br>(14:30-17:15) | Contents (Tentative)  |
|----|---------------------------|---|
| 1  | Sep 8                     | Manifolds: Definition and Examples; Smooth Maps;<br>Tangent Spaces; Differentials       |
| 2  | Sep 15                    | Submersion; Immersion; Embedding and Submanifolds;<br>Sard's Theorem                    |
| 3  | Sep 22                    | Partition of Unity; Whitney Embedding Theorem;<br>Vector Fields; Integral Curves; Flows |
| 4  | Sep 29                    | Derivation; Lie Brackets; Lie Derivatives   |
| 5  | Oct 6                     | Distributions and Frobenius Theorem   |
| 6  | Oct 13                    | Lie Groups and Lie Algebras   |
| 7  | Oct 20                    | Multi-linear Algebra; Vector Bundles  |
| 8  | Oct 27                    | Differential Forms; Exterior Derivative; Orientations                                   |
| 9  | Nov 3                     | Integration on Smooth Manifolds; Stokes' Theorem  |
| 10 | Nov10                     | De Rham Cohomology: Definition, Homotopy<br>Invariance and Mayer-Vietoris Sequence      |
| 11 | Nov 17                    | Cohomology with Compact Support;<br>Degree Theory; Poincare Duality                     |
| 12 | Nov 24 (no class)         |   |
| 13 | Dec 1                     | Poincare Duality; Sheaf Theory  |
| 14 | Dec 8                     | Cech Cohomology   |