

CENG3420

Lab 1-3: Quick Sort

Yang BAI

Department of Computer Science and Engineering
The Chinese University of Hong Kong

ybai@cse.cuhk.edu.hk

Spring 2021



香港中文大學
The Chinese University of Hong Kong

Last Time

Array Definition

```
.data
```

```
a: .word 1 2 3 4 5
```

a is the address of the first element

Branch

jal (PC is stored in ra if you specify ra)

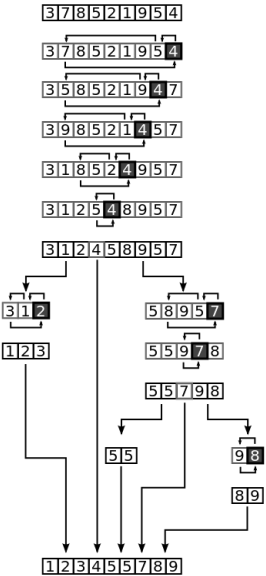
```
j jr beq blt bgt
```



Quick Sort

Quick Sort Overview

Quicksort is a **divide and conquer** algorithm. Quicksort first divides a large array into two smaller sub-arrays: the low elements and the high elements. Quicksort can then recursively sort the sub-arrays.



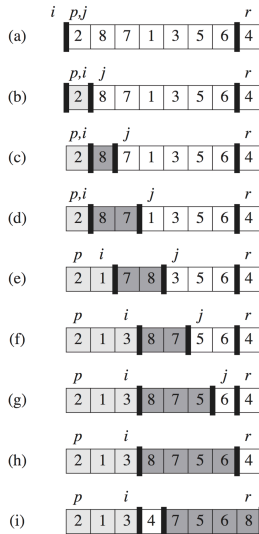
Quick Sort: Partitioning

- ▶ Pick an element, called a pivot, from the array.
- ▶ Reorder the array so that all elements with values less than the pivot come before the pivot, while all elements with values greater than the pivot come after it (equal values can go either way).

```
1: function PARTITION(A, lo, hi)
2:   pivot ← A[hi]
3:   i ← lo-1;
4:   for j = lo; j ≤ hi-1; j ← j+1 do
5:     if A[j] ≤ pivot then
6:       i ← i+1;
7:       swap A[i] with A[j];
8:     end if
9:   end for
10:  swap A[i+1] with A[hi];
11:  return i+1;
12: end function
```



Example of Partition



*

*In this example, $p = lo$ and $r = hi$.



Quick Sort: Sorting

- ▶ Recursively apply the partition to the sub-array of elements with smaller values and separately to the sub-array of elements with greater values.

```
1: function QUICKSORT(A, lo, hi)
2:   if lo < hi then
3:     p ← partition(A, lo, hi);
4:     quicksort(A, lo, p - 1);
5:     quicksort(A, p + 1, hi);
6:   end if
7: end function
```



Compiling a Recursive Procedure

A procedure for calculating factorial

```
int fact (int n)
{
    if (n < 1) return 1;
    else return (n * fact (n-1));
}
```

- ▶ A recursive procedure (one that calls itself!)

```
fact (0) = 1
fact (1) = 1 * 1 = 1
fact (2) = 2 * 1 * 1 = 2
fact (3) = 3 * 2 * 1 * 1 = 6
fact (4) = 4 * 3 * 2 * 1 * 1 = 24
. . .
```

- ▶ Assume n is passed in `a0`; result returned in `ra`



Compiling a Recursive Procedure (cont.)

```
fact:
    addi sp, sp, -8      # adjust the stack pointer
    sw   ra, 4(sp)      # save the return address
    sw   a0, 0(sp)      # save the argument 'n'
    slti t0, a0, 1      # test for 'n' < 1
    beq  t0, zero, L1   # if 'n' >=1, go to L1
    addi t1, zero, 1    # else return 1 in t1
    addi sp, sp, 8      # adjust stack pointer
    jr   ra             # return to caller

L1:
    addi a0, a0, -1     # 'n' >=1, so decrease n
    jal  fact           # call fact with (n-1)
                                # this is where fact returns

bk_f:
    lw   a0, 0(sp)      # restore argument n
    lw   ra, 4(sp)      # restore return address
    addi sp, sp, 8      # adjust stack pointer
    mul  t1, a0, t1     # t1 = n * fact(n-1)
    jr   ra             # return to caller
```



Lab Assignment

Quick Sort the following array in ascending order:

Sort the array for this assignment

-1 22 8 35 5 4 11 2 1 78

Submission Method:

Prepare a package onto [blackboard](#), including

- ▶ All source codes (<name-sid>-lab1-x.asm)
- ▶ A lab report (<name-sid>-lab1.pdf) with [step-by-step algorithm of quicksort](#) and [all console results](#).
- ▶ Deadline: [23:59, 7 March](#)

