

# Routability-Driven and Fence-Aware Legalization for Mixed-Cell-Height Circuits

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# Outline

Introduction

Multi-row Global Legalization

Max Displacement Optimization

Fixed-Row-and-Order Optimization

Experimental Results

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# Motivation

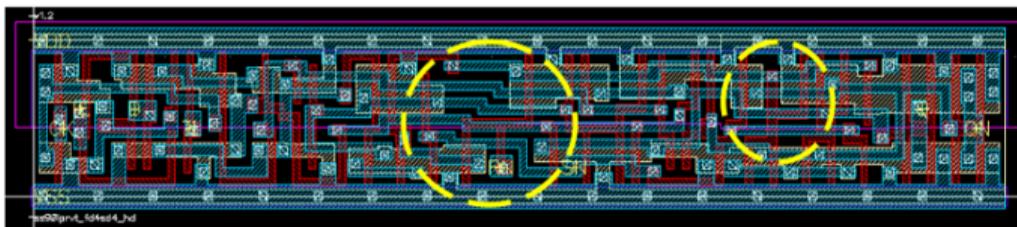


Figure 1: Large Single-Row Cell [Baek et al. 2008]

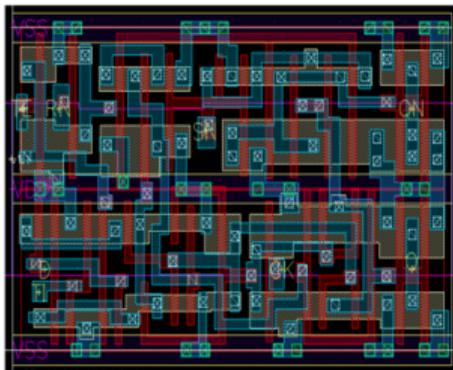


Figure 2: Multi-Row Cell [Baek et al. 2008]

- ▶ Cells like multi-bit flip-flops (MBFFs) occupy multiple rows <sup>a</sup>.
- ▶ Cells are much more accessible by being modified to be multi-row height <sup>b</sup>.

<sup>a</sup>[Lin, Hsu, and Chang 2011]

<sup>b</sup>[Raghavan et al. 2016]

# Legalization

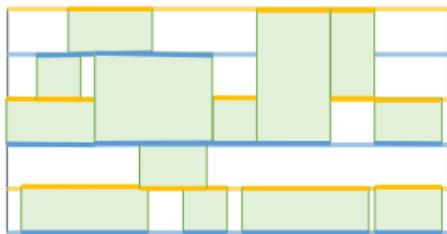


Figure 3: Power/ground alignment.

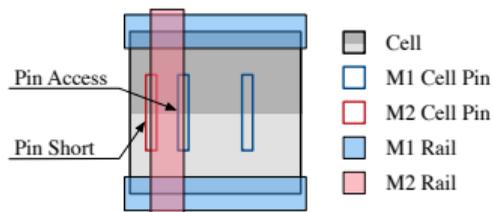


Figure 4: Pin access and pin short.

Objective function <sup>a</sup>:

$$S_{am} = \frac{1}{H} \sum_{h=1}^H \frac{1}{|C_h|} \sum_{c_i \in C_h} \delta_i, \quad (1)$$

where  $\delta_i = \delta_{x_i} + \delta_{y_i} = |x_i - x'_i| + |y_i - y'_i|$ , satisfying <sup>b</sup>:

- ▶ Cells are overlap-free;
- ▶ Cells are aligned to placement sites.
- ▶ Cells with height of even multiples of site height must be placed in alternate rows with matching power and ground alignment.
- ▶ Signal pins of cells should not be short or inaccessible due to the P/G grids and IO pins <sup>c</sup>.

<sup>a</sup>[Darav, Bustany, et al. 2017]

<sup>b</sup>[Chow, Pui, and Young 2016]

<sup>c</sup>[Darav, Kennings, et al. 2016]



# Detailed Placement Flow

The detailed placement consists of three stages.

- ▶ Inserts the cells sequentially into the placement region.
- ▶ Optimize the maximum displacement by swapping cells.
- ▶ Further optimize the average and maximum displacement.

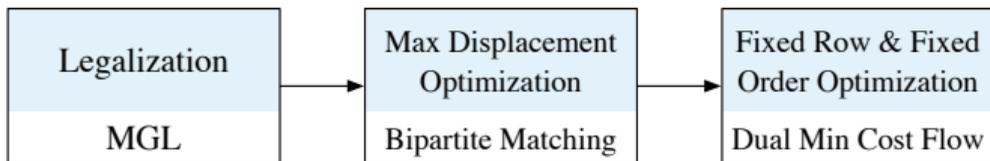


Figure 5: Detailed placement flow.

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# [Chow, Pui, and Young 2016]

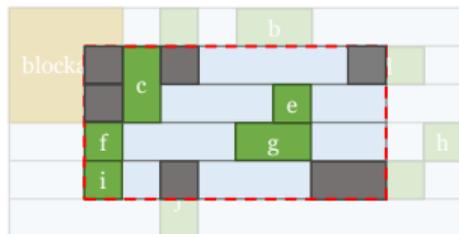


Figure 6: Local Region

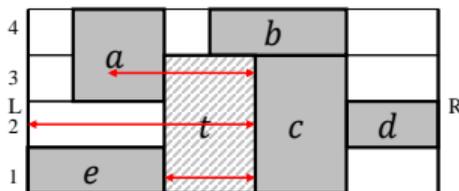


Figure 7: Insertion Point

- ▶ Define local region
- ▶ Enumerate insertion points
- ▶ Evaluate cost
- ▶ Spread overlapping cells

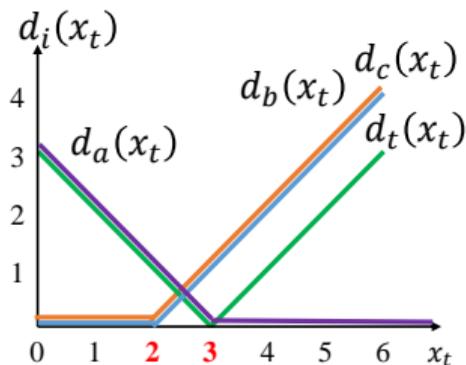


Figure 8: Cost Evaluation

# Difference between MLL & MGL

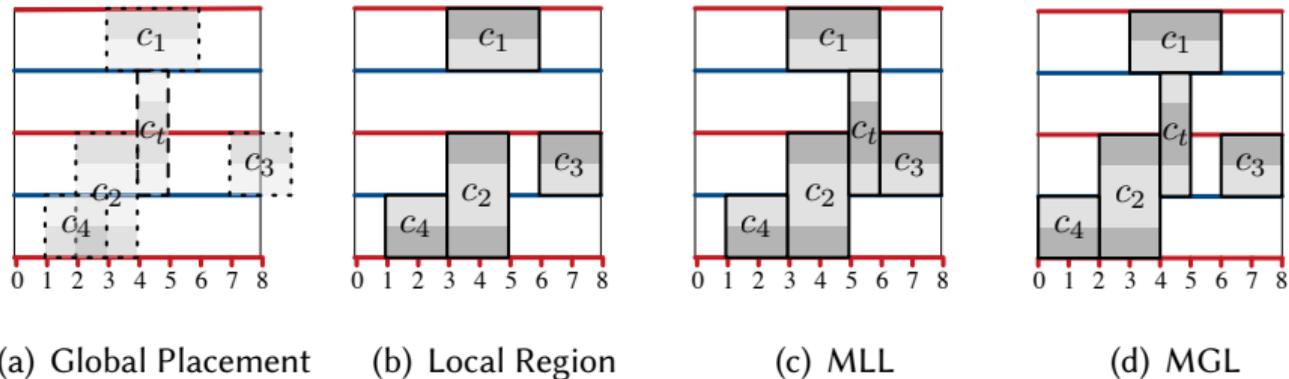
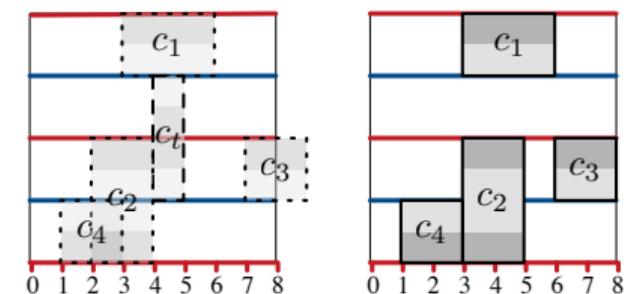


Figure 9: Comparison between MLL and MGL.

**MLL** optimizes the total displacement from the initial positions of the cells in the window before calling MLL.

**MGL** minimizes the displacement from the respective positions of cells obtained after global placement.

# Clustered Cells



(a) Global Placement      (b) Local Region

Figure 10:  $c_2$  and  $c_4$  form a cluster.

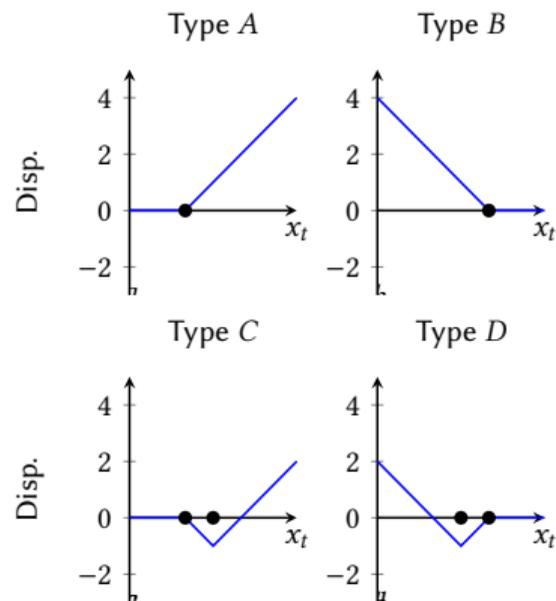


Figure 11: Cost Curve Types A – D.

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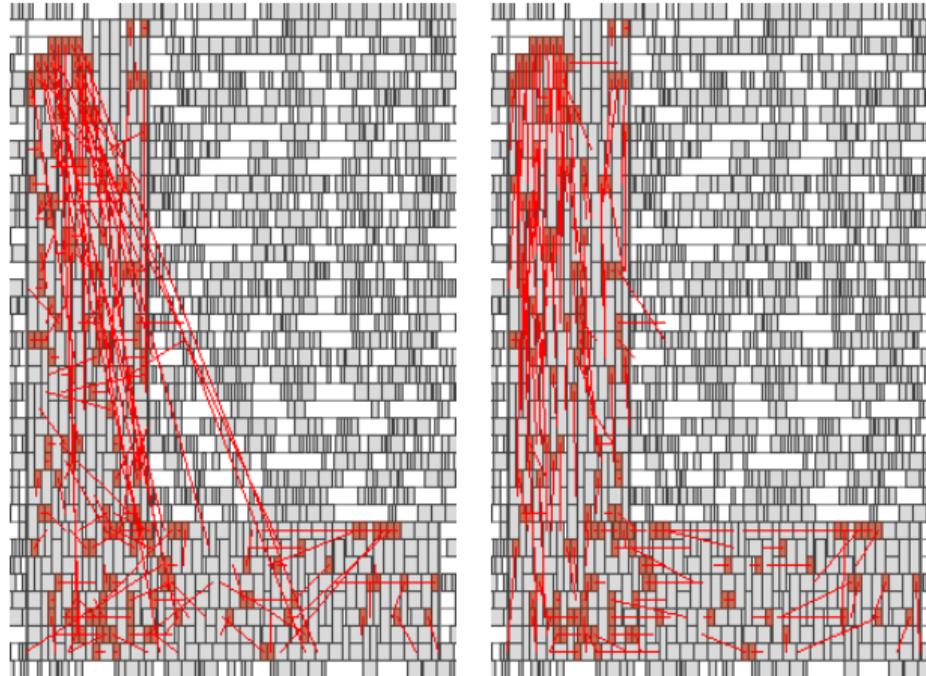
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# Bipartite Matching



(a) Before

(b) After

Figure 12: Bipartite matching.

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# [Vygen 1998]

- ▶ Fixed-row and fixed-order.
- ▶ Minimizes the half-perimeter wire length (HPWL).
- ▶ A dual of min-cost flow problem.

# Fixed Row & Fixed Order Optimization

Formulate linear displacement:

$$\max_{x_i, x_i^-, x_i^+} \sum_i n_i(x_i^- - x_i^+) \quad (2)$$

$$\text{s.t. } x_i^- \leq x_i - x_i' \leq x_i^+, \quad \forall c_i \in C, \quad (2a)$$

$$x_i^- \leq 0 \leq x_i^+, \quad \forall c_i \in C, \quad (2b)$$

$$x_i - x_j \leq -w_i, \quad \forall (i, j) \in E, \quad (2c)$$

$$l_i \leq x_i \leq r_i, \quad \forall c_i \in C. \quad (2d)$$

Let  $\tilde{x}^0$  be the absolute position of the *origin*, then the absolute positions  $\{\tilde{x}_i, \tilde{x}_i^-, \tilde{x}_i^+\}$  of  $\{x_i, x_i^-, x_i^+\}$  are  $\tilde{x}_i = x_i + \tilde{x}^0$ ,  $\tilde{x}_i^- = x_i^- + \tilde{x}^0$ ,  $\tilde{x}_i^+ = x_i^+ + \tilde{x}^0$ . Thus,

$$\max_{\tilde{x}_i, \tilde{x}_i^-, \tilde{x}_i^+, \tilde{x}^0} \sum_i n_i(\tilde{x}_i^- - \tilde{x}_i^+) \quad (3)$$

$$\text{s.t. } \tilde{x}_i^- \leq \tilde{x}_i - x_i' \leq \tilde{x}_i^+, \quad \forall c_i \in C, \quad (3a)$$

$$\tilde{x}_i^- - \tilde{x}^0 \leq 0 \leq \tilde{x}_i^+ - \tilde{x}^0, \quad \forall c_i \in C, \quad (3b)$$

$$\tilde{x}_i - \tilde{x}_j \leq -w_i, \quad \forall (i, j) \in E, \quad (3c)$$

$$l_i \leq \tilde{x}_i - \tilde{x}^0 \leq r_i, \quad \forall c_i \in C, \quad (3d)$$

whose dual linear programming is a min-cost flow problem.



# Example of Min-Cost Flow

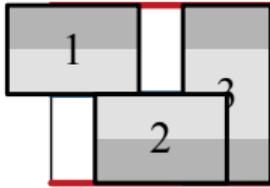


Figure 13: GP.

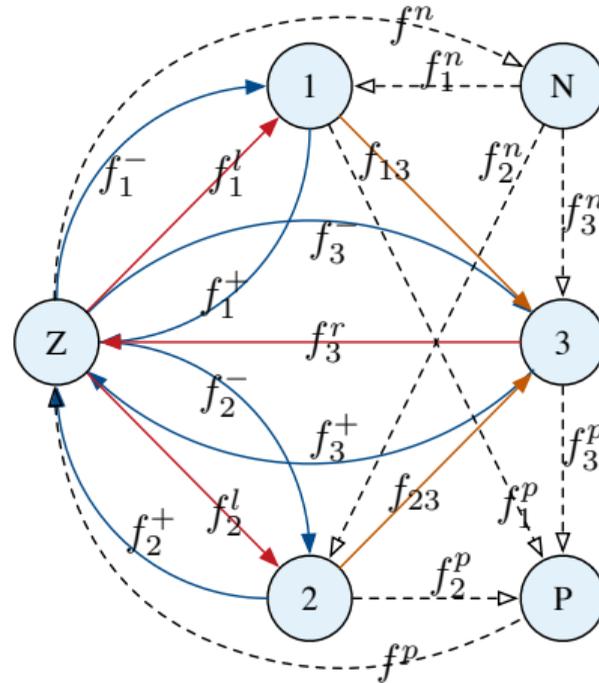


Figure 14: Flow network.

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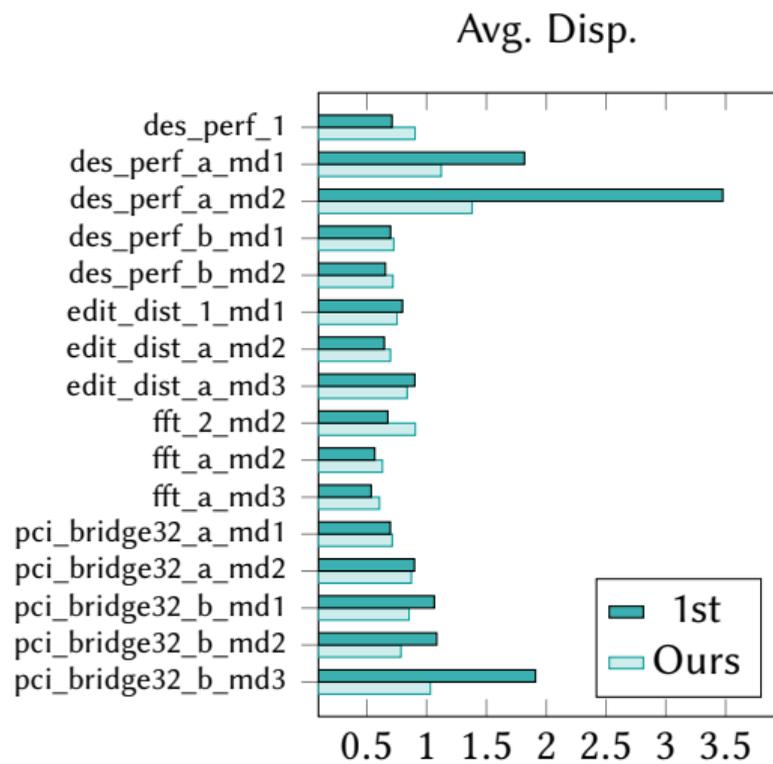
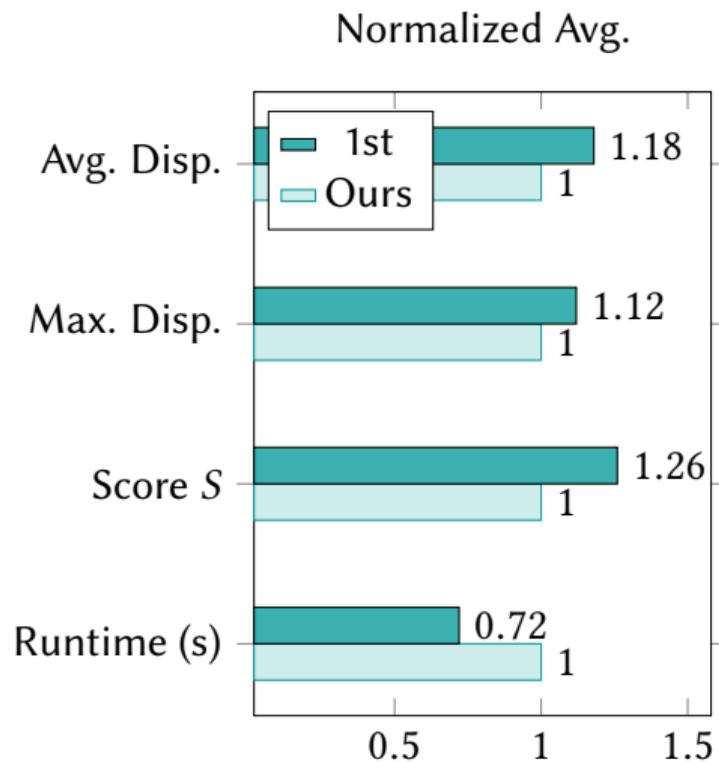
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# Experimental Results



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# Conclusion

- ▶ Propose multi-row global legalization.
- ▶ Adjust the maximum displacement by bipartite matching.
- ▶ Formulate the fix-row-and-order legalization into a minimum-cost flow problem.
- ▶ Comparing with the champion of the ICCAD 2017 Contest, we achieved 18% less average displacement, 12% less maximum displacement, and much fewer routability-driven violations.

Thanks!

Questions?



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