

CSCI3610: Special Exercise Set 3

Problem 1. If we run the activity-selection algorithm taught in the class on the following input:
 $S = \{[1, 10], [2, 22], [3, 23], [20, 30], [25, 45], [40, 50], [47, 62], [48, 63], [60, 70]\}$
what is the set of intervals returned?

Problem 2. The following is another greedy algorithm for the activity selection problem. Initialize an empty T , and then repeat the following steps until S is empty:

- (Step 1) Add to T the interval I with the shortest length.
- (Step 2) Remove from S the interval I , and all the intervals overlapping with I .

Finally, return T as the answer.

Prove: the above algorithm does not always return an optimal solution.

Problem 3 (0-1 Knapsack). Suppose that there are n gold bricks, where the i -th piece weighs p_i pounds and is worth d_i dollars. Given a positive integer W , our goal is to find a set S of gold bricks such that

- the total weight of the bricks in S is at most W , and
- the total value of the bricks in S is maximized (among all the sets S satisfying the first condition).

Assuming $d_1 \geq d_2 \geq \dots \geq d_n$, let us consider the following greedy algorithm:

1. $S = \emptyset$
2. **for** $i = 1$ to n
3. **if** $p_i \leq W$ **then**
4. add p_i to S ; $W \leftarrow W - p_i$

Prove: the above algorithm does not guarantee finding the desired set S .