

**Corollary 2.30 (Fundamental Inequality)** For any  $a > 0$ ,

$$\ln a \leq 1 - \frac{1}{a}$$

with equality if and only if  $a = 1$ .