

**Lemma 2.29 (Fundamental Inequality)** For any  $a > 0$ ,

$$\ln a \leq a - 1$$

with equality if and only if  $a = 1$ .