

Proposition 2.5 For random variables X, Y , and Z , $X \perp Z|Y$ if and only if

$$p(x, y, z) = a(x, y)b(y, z)$$

for all x, y , and z such that $p(y) > 0$.