

Theorem Let X, X', Y , and Y' be real random variables such that f_{XY} and $f_{X'Y'}$ exist, and $f_{Y|X} = f_{Y'|X'}$. Then

$$D(f_X || f_{X'}) \geq D(f_Y || f_{Y'}).$$

Proof Exercise.