

$$\psi_i(t) = \sqrt{2N} \sin(2Nt - i)$$