

**Definition 11.16** The mutually typical set  $\Psi_{[XY]}^n$  with respect to  $F(x, y)$  is the set of  $(\mathbf{x}, \mathbf{y}) \in \mathcal{X}^n \times \mathcal{Y}^n$  such that

$$\left| \frac{1}{n} \log \frac{f(\mathbf{y}|\mathbf{x})}{f(\mathbf{y})} - I(X; Y) \right| \leq \delta,$$

where

$$f(\mathbf{y}|\mathbf{x}) = \prod_{i=1}^n f(y_i|x_i) \quad \text{and} \quad f(\mathbf{y}) = \prod_{i=1}^n f(y_i),$$

and  $\delta$  is an arbitrarily small positive number. A pair of sequences  $(\mathbf{x}, \mathbf{y})$  is called mutually  $\delta$ -typical if it is in  $\Psi_{[XY]}^n$ .