

**Proposition 10.9 (Preservation of Energy)** Let  $\mathbf{Y} = Q\mathbf{X}$ , where  $Q$  is an orthogonal matrix. Then

$$E \sum_{i=1}^n Y_i^2 = E \sum_{i=1}^n X_i^2.$$