CSCI 3130 Formal Languages and Automata Theory

## Week 4 Tutorial Session

- 1. For any integer  $k \ge 0$ , define  $L_k = \{ww \mid w \in \{0, 1\}^k\}$ .
  - (a) Write down all strings in  $L_3$ .
  - (b) Prove that any DFA for  $L_k$  has at least  $2^k$  states.
- 2. For an integer  $k \ge 1$ , define  $L_k$  to be the set of strings (over  $\Sigma = \{0, 1\}$ ) that have a 1 at the kth-to-last position. For example, **1**00 and **0101** are in  $L_3$ , but 0 and **0111** are not.
  - (a) Prove that every DFA for  $L_k$  has at least  $2^k$  states.
  - (b) Describe (e.g. with a diagram) an NFA for  $L_k$  that has at most k+1 states.
- 3. Let L be the set of strings over  $\{0, 1\}$  whose number of ones is a perfect square (e.g. 0, 1, 4, 9, 16, ...). Prove that L is irregular.