

Week 11 Tutorial Session

- (1) Show that the following languages are decidable.
- (a) $L_1 = \{\langle R \rangle \mid R \text{ generates at least one string } w \text{ that has } 111 \text{ as a substring}\}$
Here R is a regular expression over alphabet $\{0, 1\}$.
 - (b) $E_{\text{CFG}} = \{\langle G \rangle \mid \text{Context-free grammar } G \text{ generates no strings } (L(G) = \emptyset)\}$
- (2) For each of these languages, say whether it is decidable. Justify your answer.
- (a) $L_1 = \{\langle M, w, t \rangle \mid \text{Turing machine } M \text{ accepts } w \text{ within } t \text{ transitions}\}$
 - (b) $L_2 = \{\langle M \rangle \mid \text{Turing machine } M \text{ recognizes strings of odd length}\}$
Recall that a Turing machine M recognizes a language L if M accepts all strings in L and nothing else.