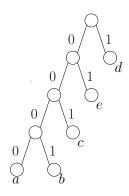
## CSCI3160: Quiz 2

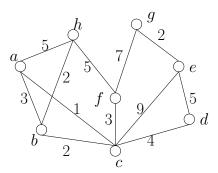
Name: Student ID

**Problem 1 (40%).** Consider the alphabet  $\Sigma$  with letters a, b, c, d, e and whose frequencies are 5%, 12%, 17%, 35% and 23% respectively. Show the prefix code tree produced by Huffman's algorithm.

Solution.



**Problem 2 (20%).** Consider running Prims' algorithm to find a minimum spanning tree (MST) of the undirected weighted graph below. Recall that the algorithm grows a tree by including one vertex each time. Suppose that the set of vertices already in the tree is  $\{a, c, b, h\}$ . What is the next vertex to be included?



Solution. f.

**Problem 3 (40%).** Consider the optimal BST problem on  $S = \{1, 2, 3, 4\}$  and the weight array (25, 15, 20, 50). Show an optimal BST on S with the smallest average cost.

**Solution.** Both solutions below have average cost 215.

